
Feedback

Transimpedance & Current

Amplifiers

Willy Sansen

KULeuven, ESAT-MICAS
Leuven, Belgium

willy.sansen@esat.kuleuven.be



Table of contents

- **Introduction**
- **Shunt-shunt FB for Transimpedance amps.**
- **Shunt-series FB for Current amplifiers**
- **Transimpedance amplifiers for
low noise and high frequencies**

Input- & output impedances

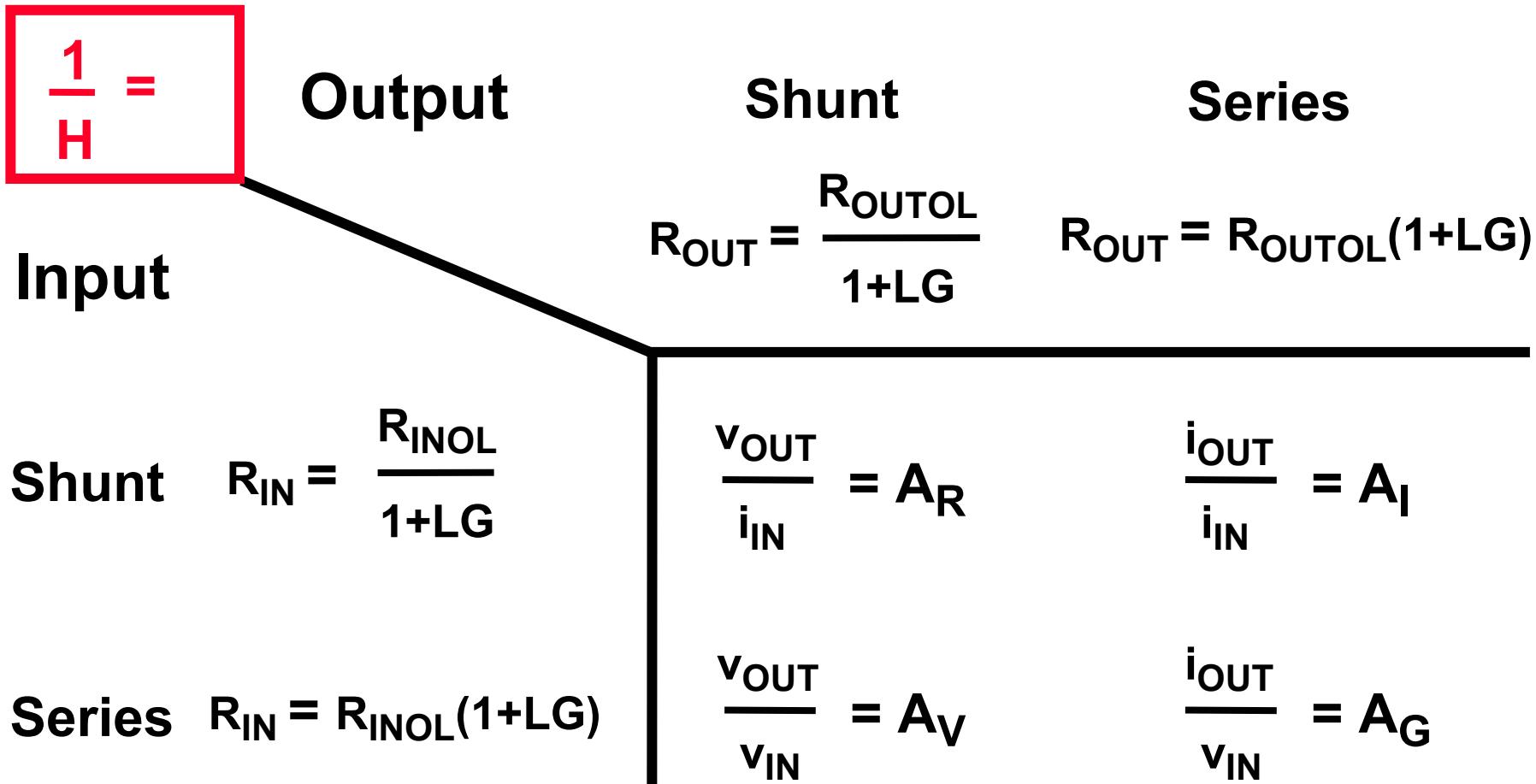
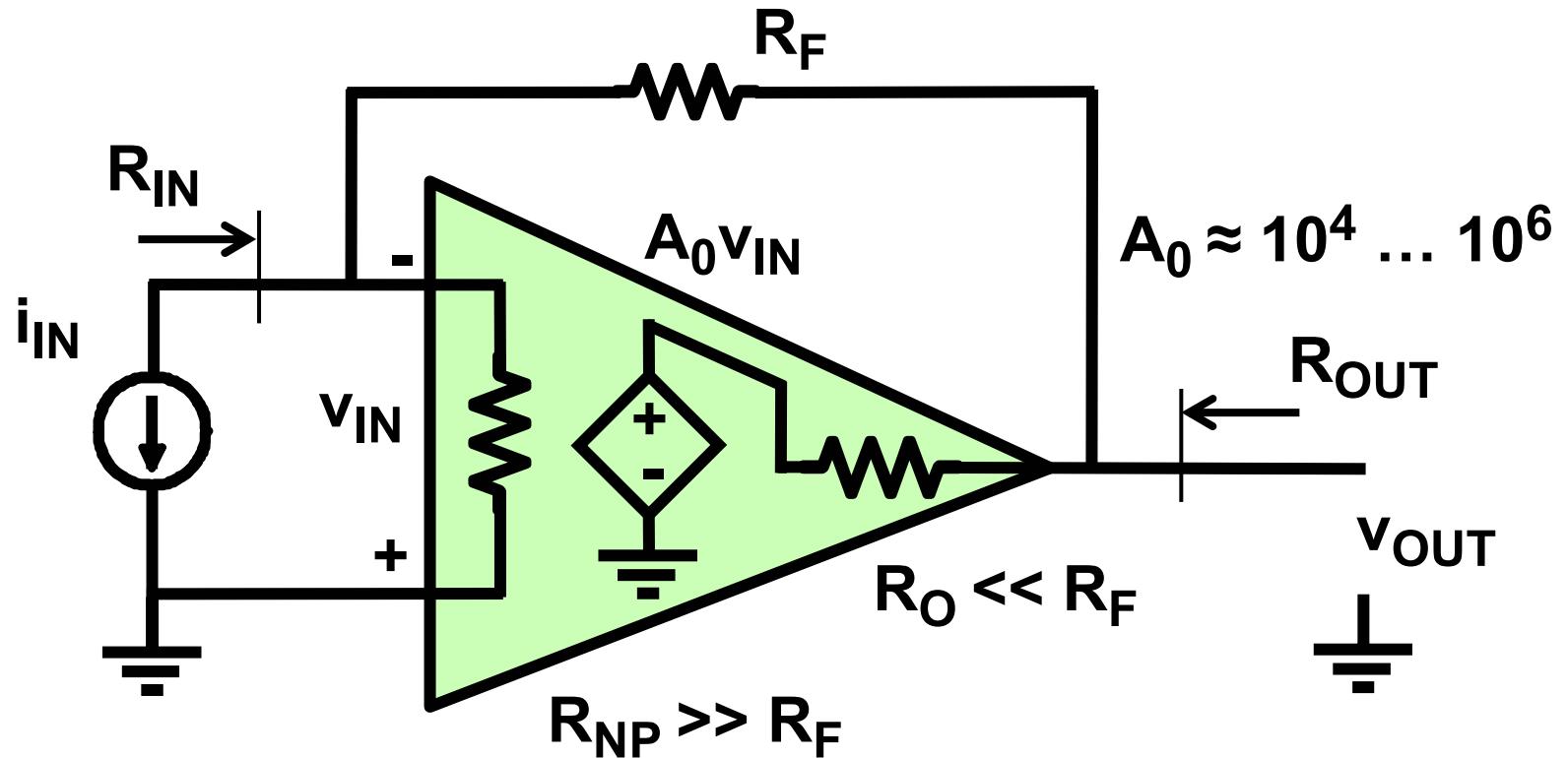


Table of contents

- Introduction
- Shunt-shunt FB for Transimpedance amps.
- Shunt-series FB for Current amplifiers
- Transimpedance amplifiers for
low noise and high frequencies

Shunt-shunt FB configuration

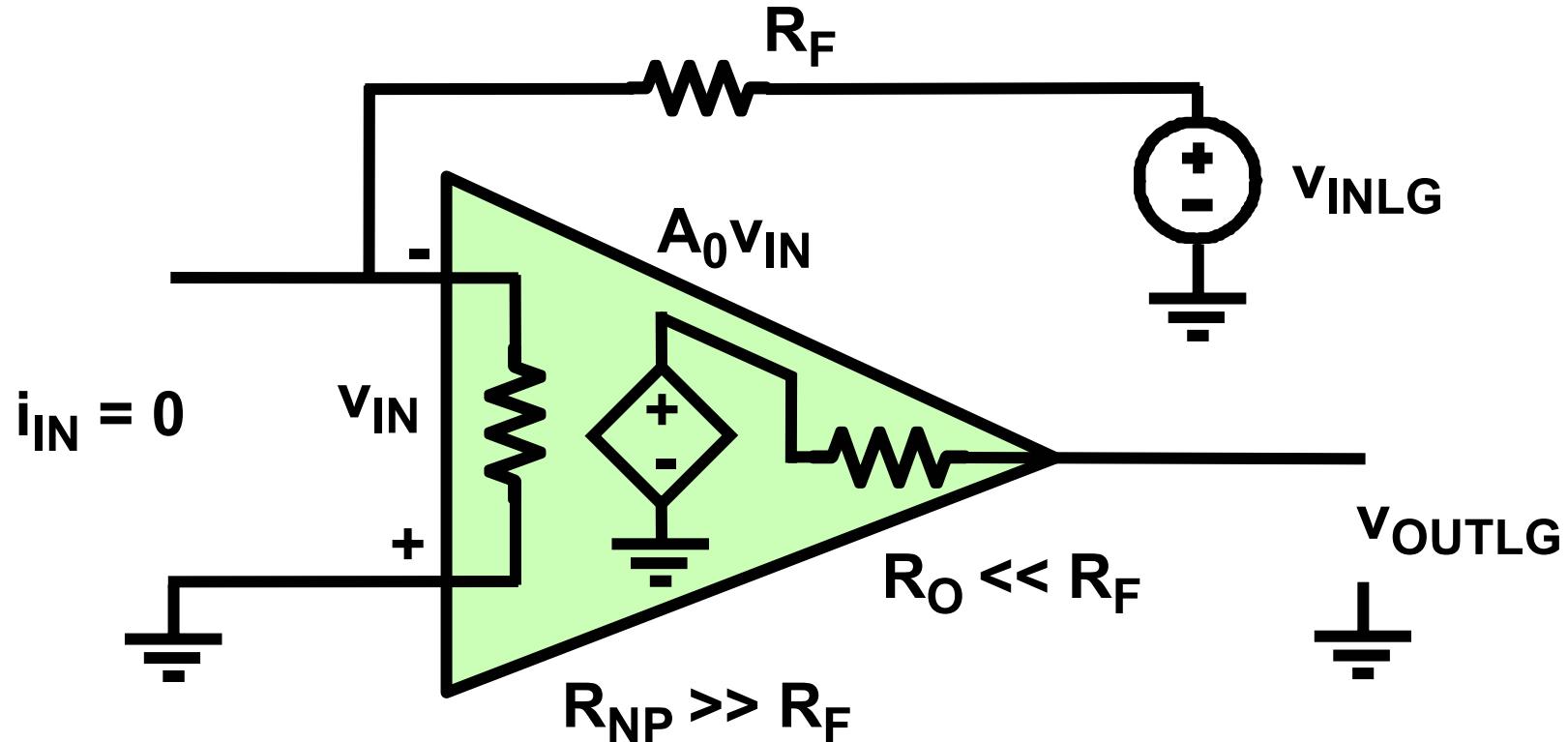


$$A_R = \frac{v_{OUT}}{i_{IN}} = R_F$$

$$R_{IN} \approx 0$$

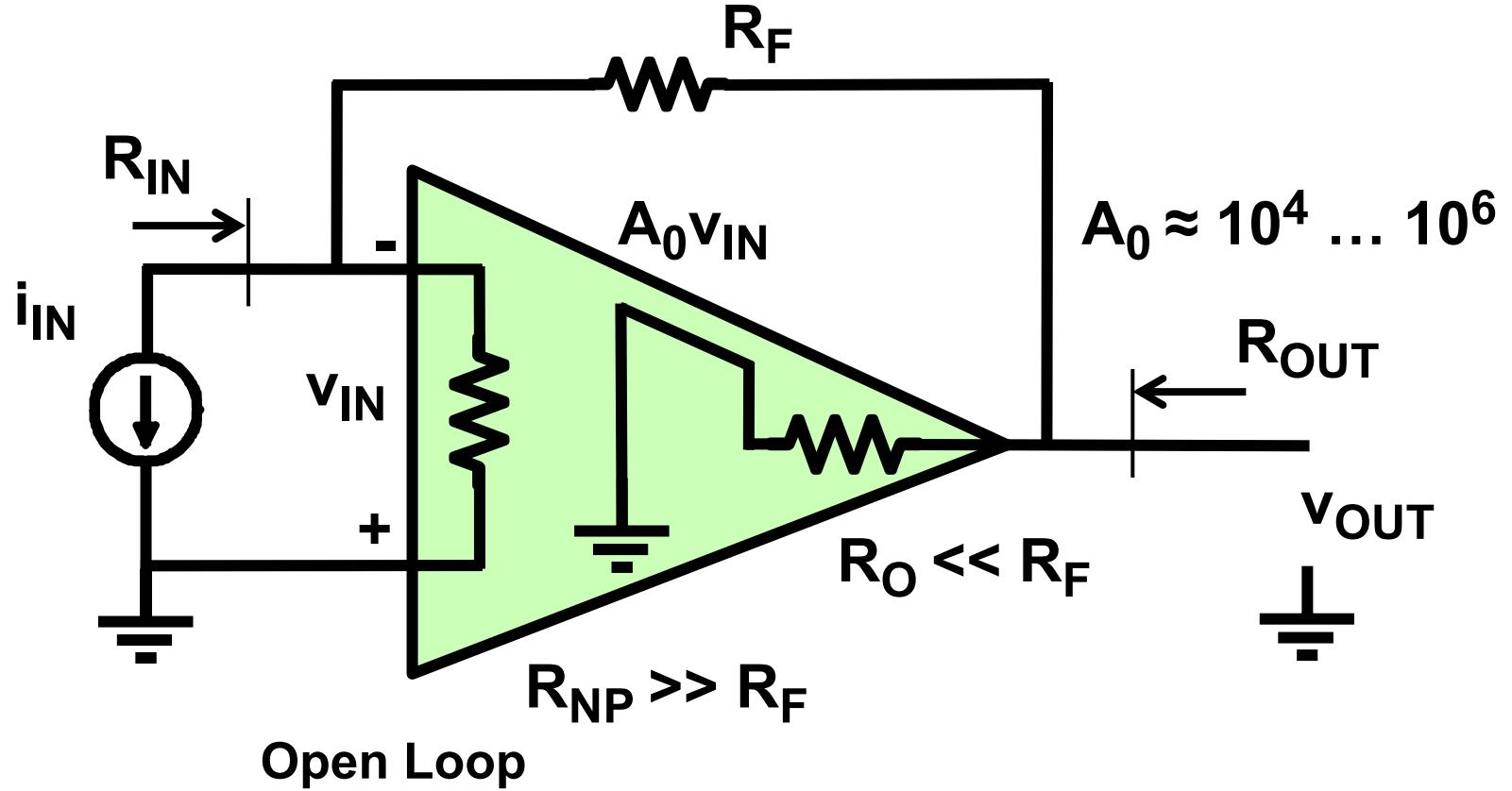
$$R_{OUT} \approx 0$$

Shunt-shunt FB : loop gain



$$LG = \frac{v_{OUTLG}}{v_{INLG}} \approx A_{vOL} \approx A_0 \approx 10^4 \dots 10^6$$

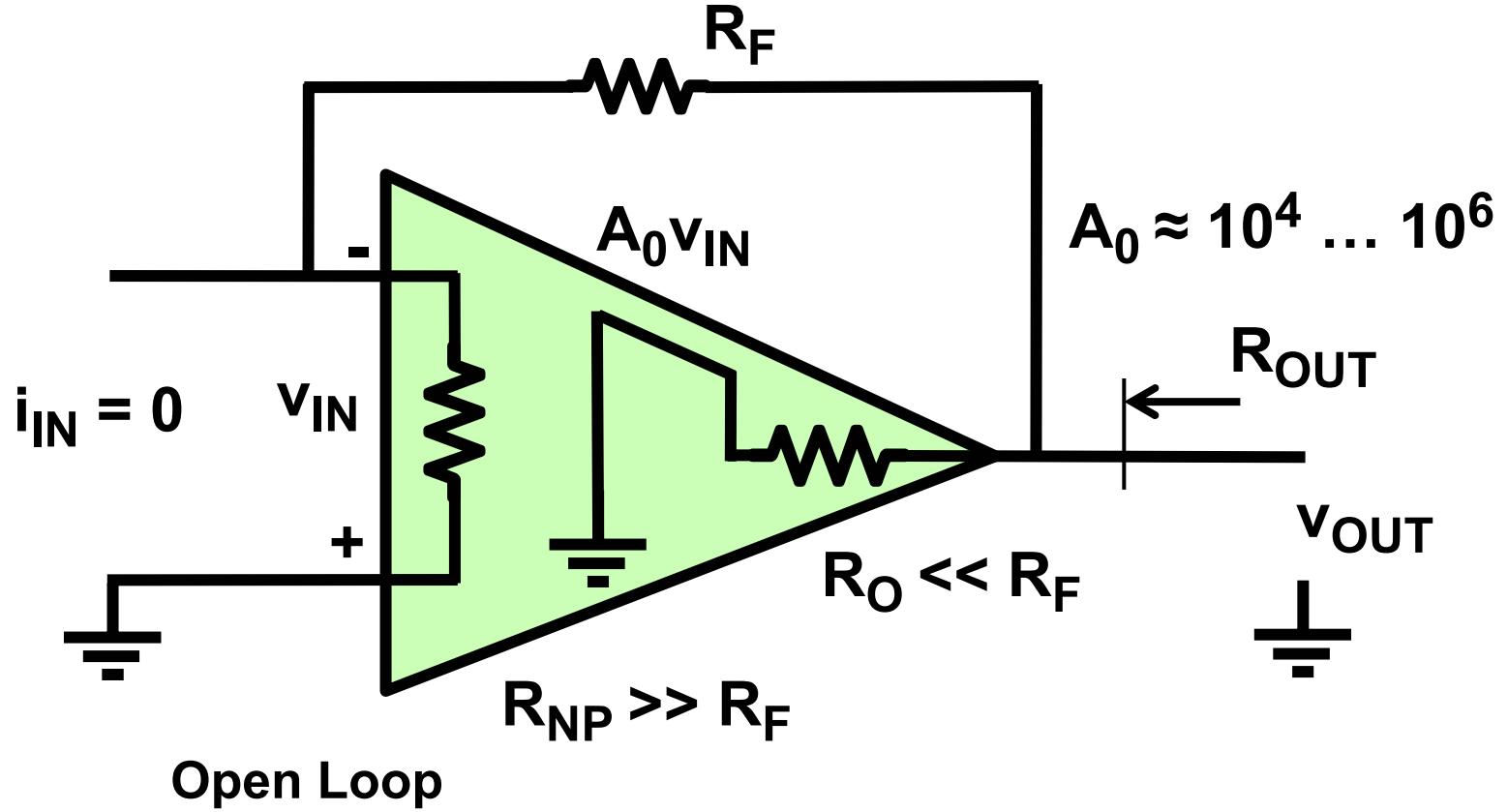
Shunt-shunt FB : input resistance



$$R_{IN} = \frac{v_{IN}}{i_{IN}} = \frac{R_{INOL}}{LG} \approx 0$$

$$R_{INOL} = R_{IN} (A_v = 0) = R_{NP} // (R_F + R_O) \approx R_F$$

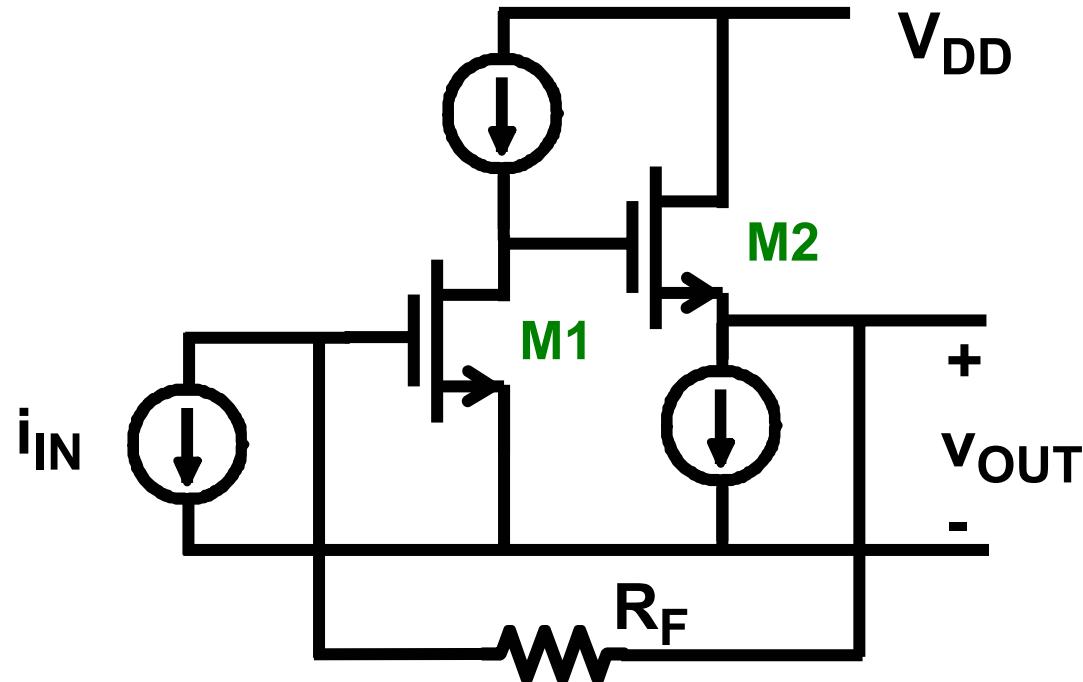
Shunt-shunt FB : output resistance



$$R_{OUT} = \frac{R_{OUTOL}}{LG} \approx 0$$

$$\begin{aligned} R_{OUTOL} &= R_{OUT} (A_v = 0) \\ &= R_O / (R_F + R_{NP}) \approx R_O \end{aligned}$$

Shunt-shunt FB pair



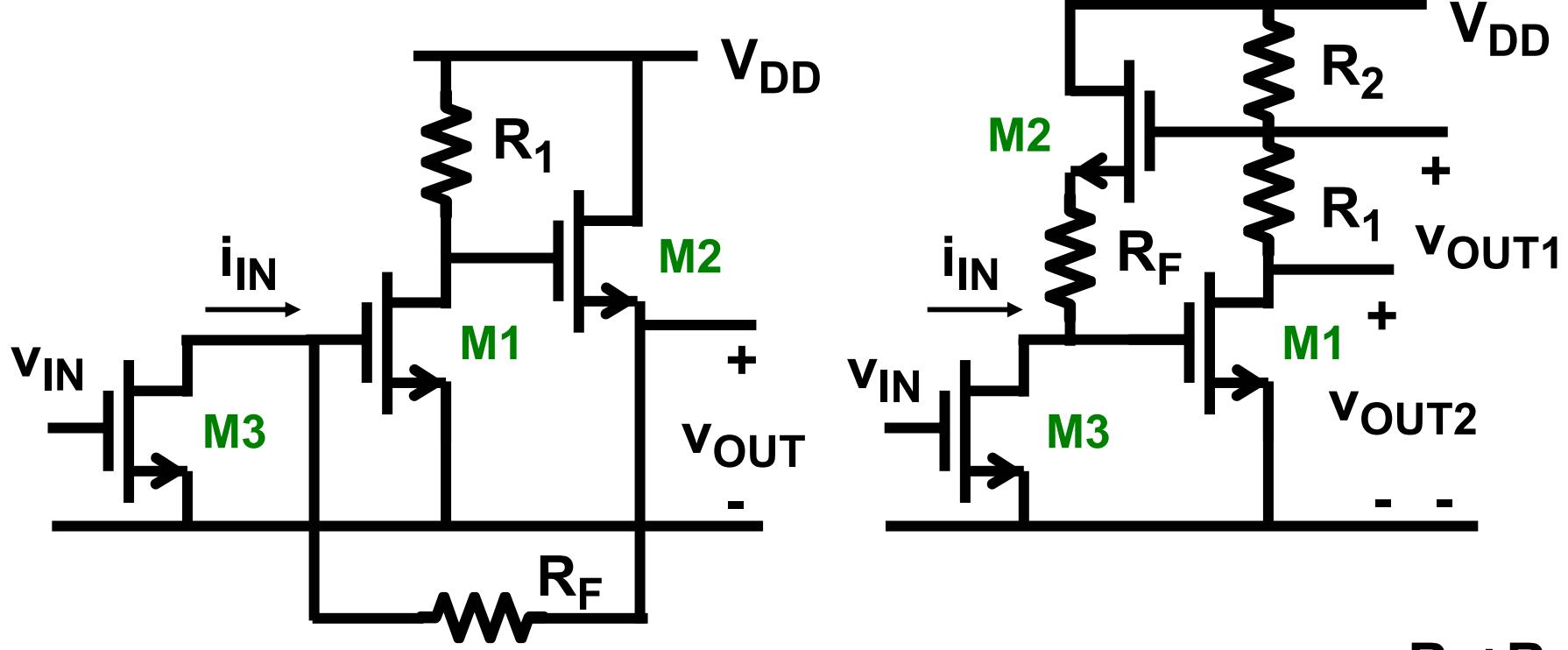
$$A_R = \frac{v_{OUT}}{i_{IN}} = R_F$$

$$LG = g_{m1}r_{o1}$$

$$R_{IN} = \frac{R_F}{LG} \approx 0 ?$$

$$R_{OUT} = \frac{1/g_{m2}}{LG} \approx 0$$

Shunt-shunt FB pair with resistors

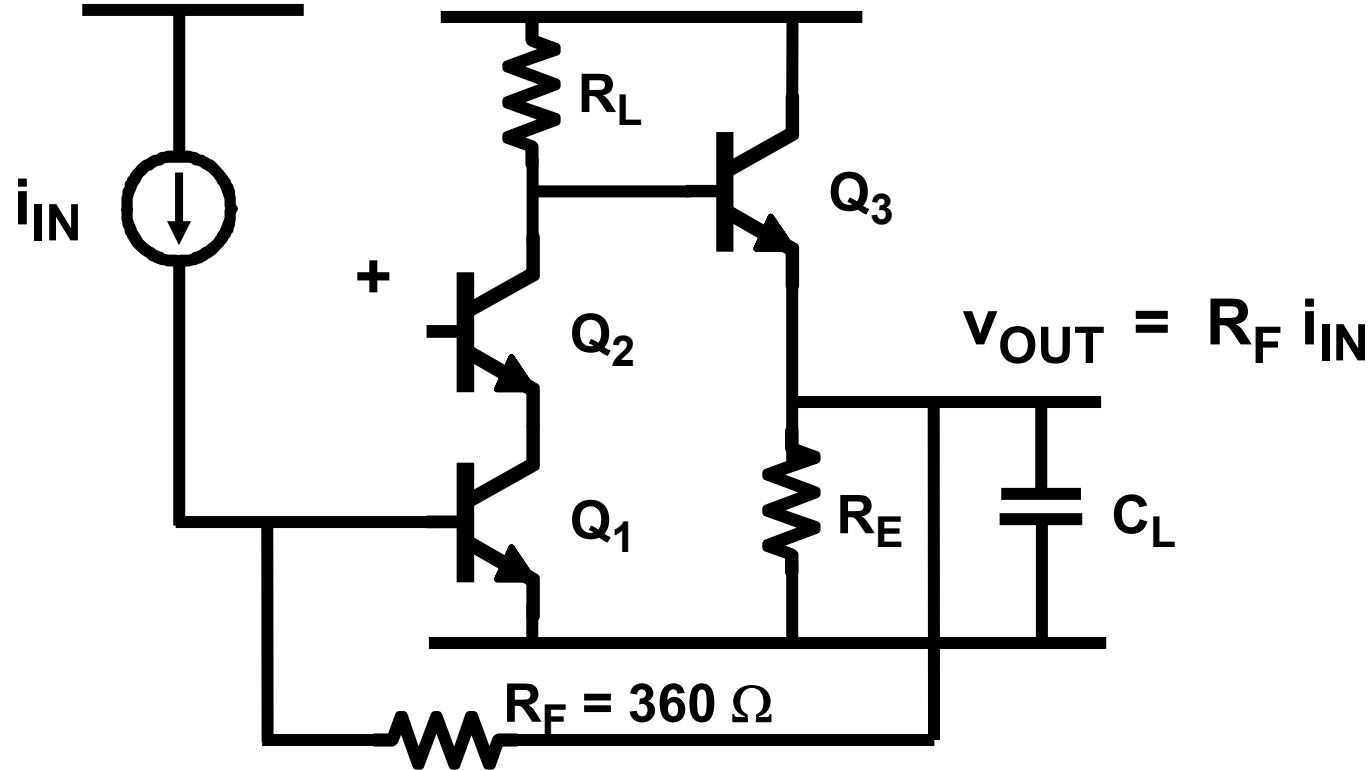


$$A_R = \frac{v_{OUT}}{i_{IN}} = R_F$$

$$A_{R1} = R_F \quad A_{R2} = R_F \frac{R_1 + R_2}{R_2}$$

Ref.Cherry, Proc. IEE, Feb.63, 375-389; Holdenried, JSSC Nov.04, 1959-1967

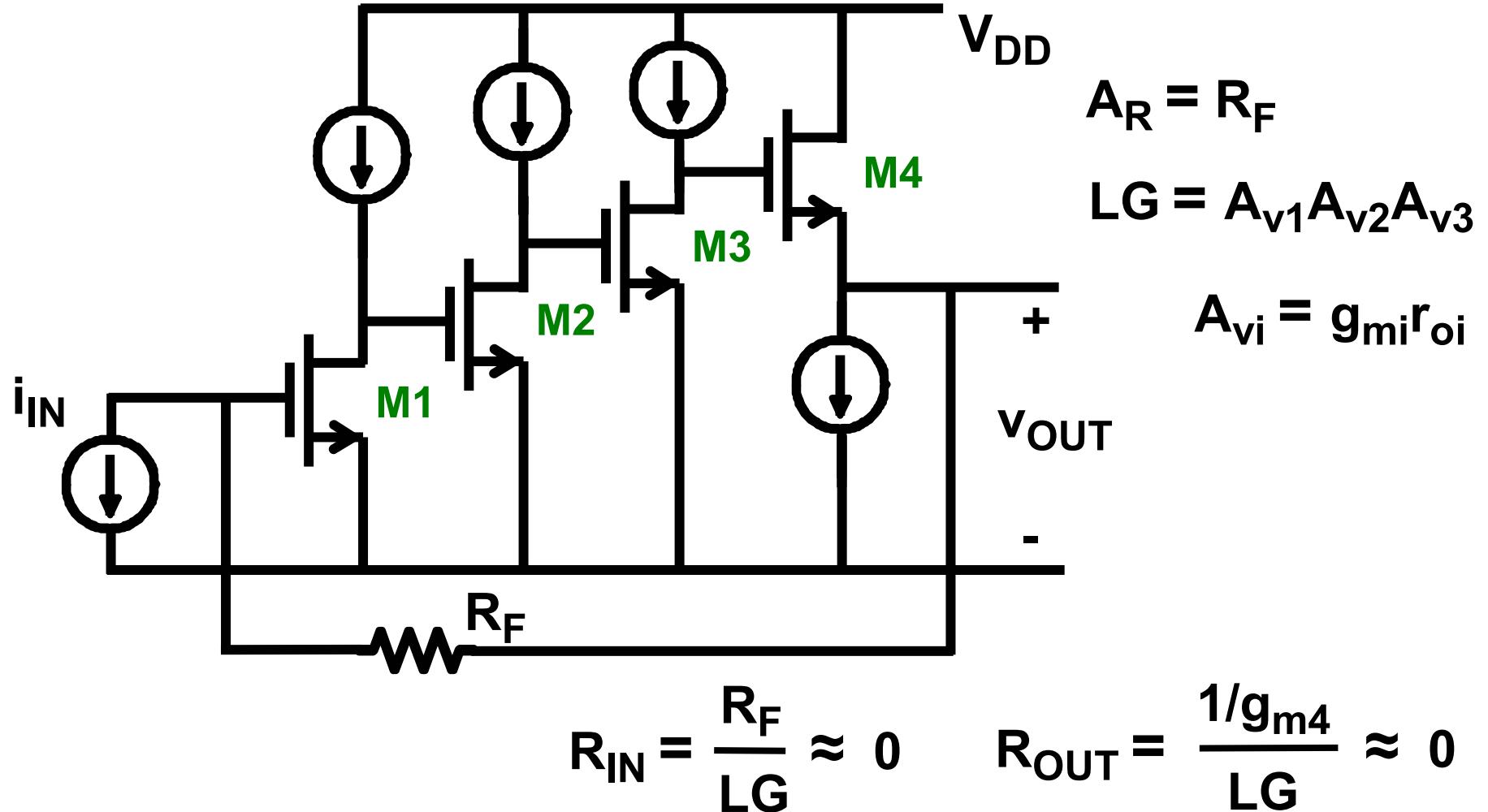
Current detector with voltage amp.



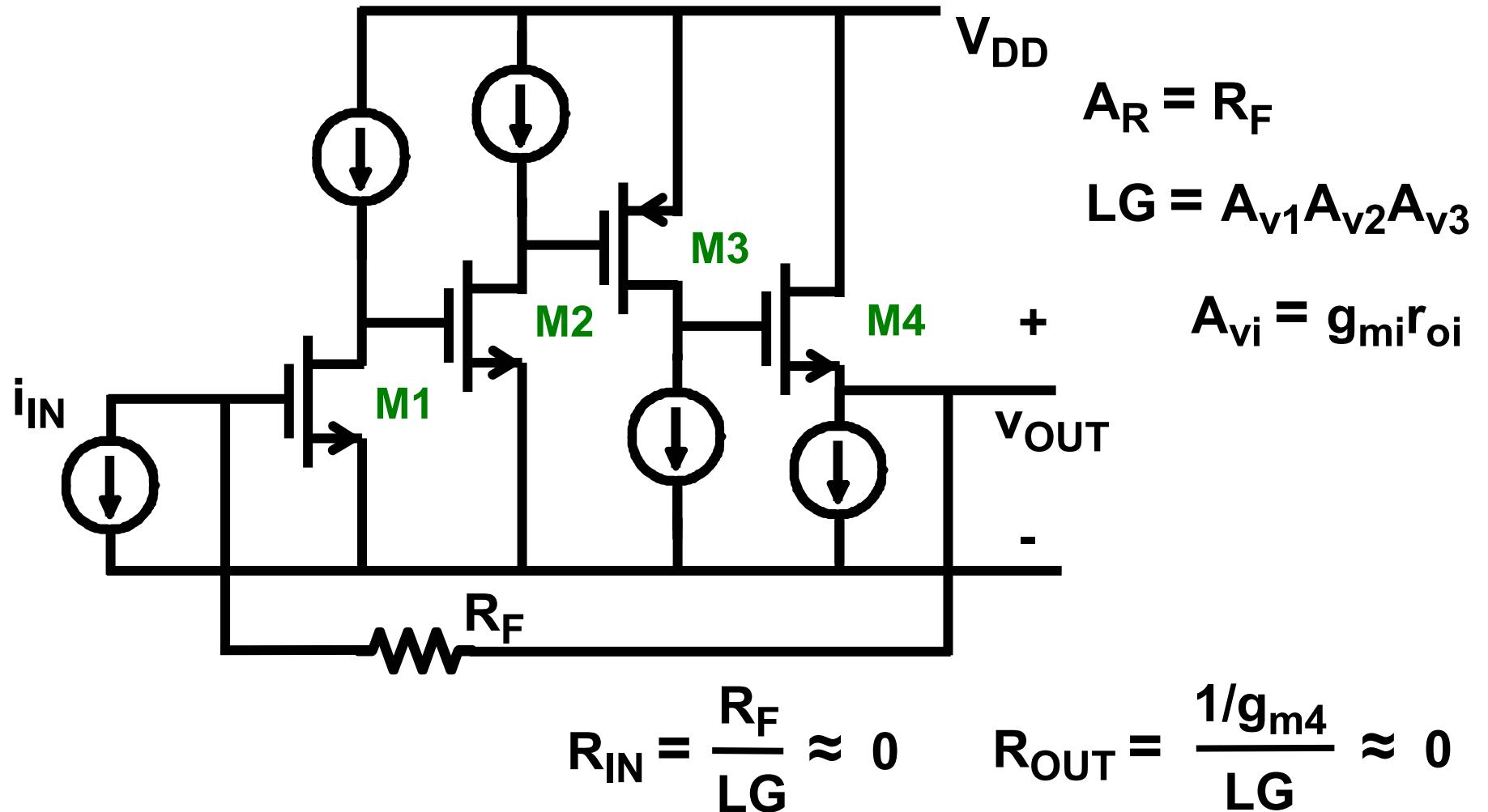
$f_T = 40 \text{ GHz}$ $r_B = 20 \Omega$ $\text{BW} = 10 \text{ GHz}$ $I_{TOT} = 10 \text{ mA}$

Ref.Baureis, JSSC
June 1993, 701-706

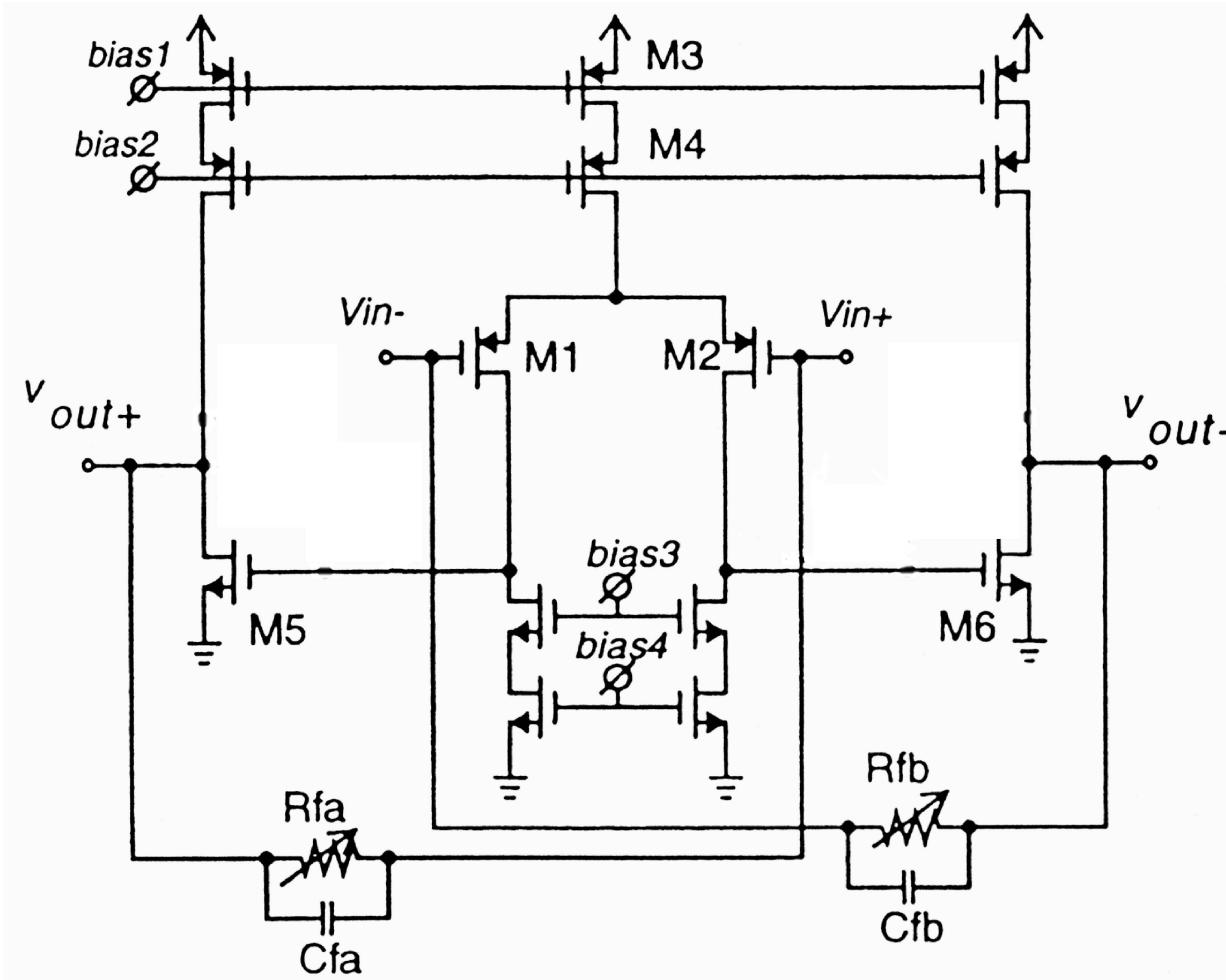
Shunt-shunt FB triple



Shunt-shunt FB triple: easier biasing



CMOS preamplifier for optical communications



Two stages
possible
if fully differential !

$20 \text{ k}\Omega \dots 500 \Omega$
tracking
of R_1 & R_f

Ref.Phang, Johns,
CAS-II July 1999

Differential shunt-shunt FB pair

$$A_R = R_F$$

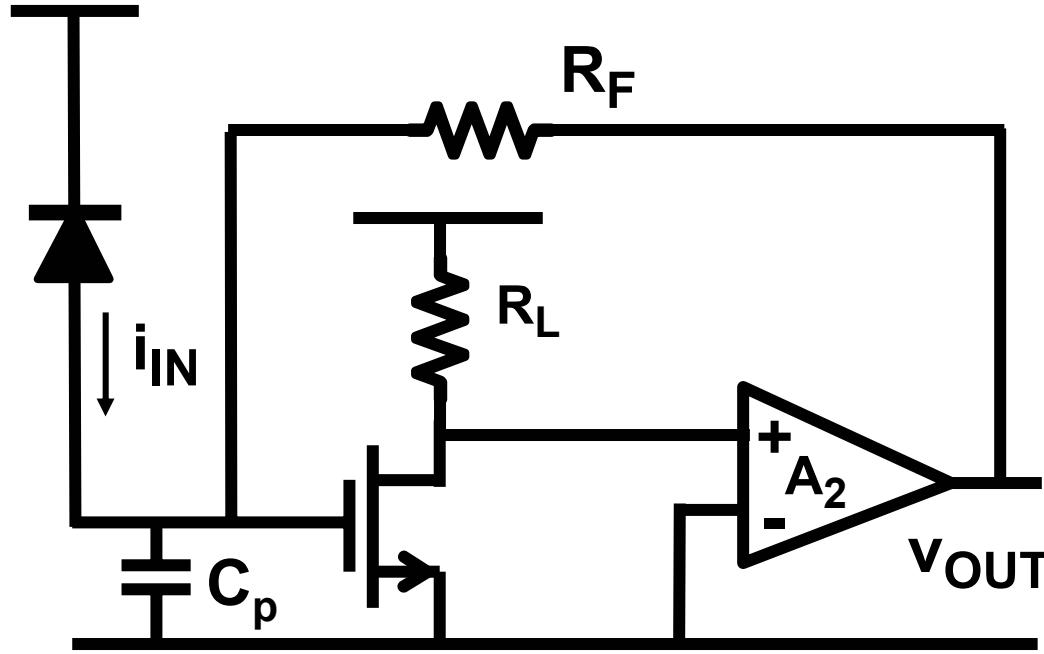
$$LG = A_{v1}A_{v2}$$

$$A_{v1} = g_{m1}r_{o1}$$

$$A_{v2} = g_{m2}r_{o2}$$

$$R_{IN} = \frac{2R_F}{LG} \approx 0 \quad R_{OUT} = \frac{2/g_{m3}}{LG} \approx 0$$

Current detector with voltage amplifier



$$A_1 = g_m R_L$$

$$A_2$$

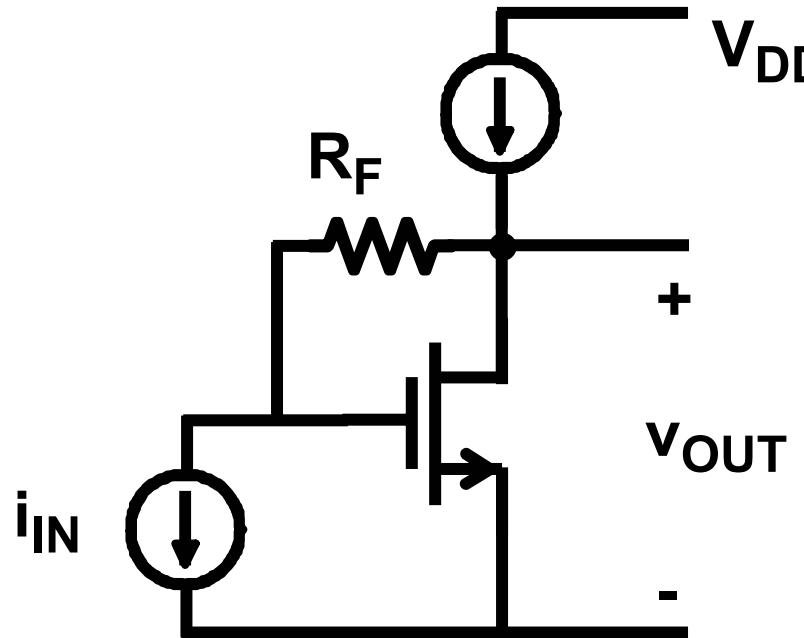
$$R_{IN} = \frac{v_{IN}}{i_{IN}} = \frac{R_F}{A_1 A_2}$$

$$A_R = \frac{v_{OUT}}{i_{IN}} = R_F$$

$$LG = A_1 A_2$$

$$f_{-3dB} = \frac{1}{2\pi R_{IN} C_p}$$

Single MOST with shunt-shunt FB



$$A_R = R_F \quad (\text{if } >> 1/g_m)$$

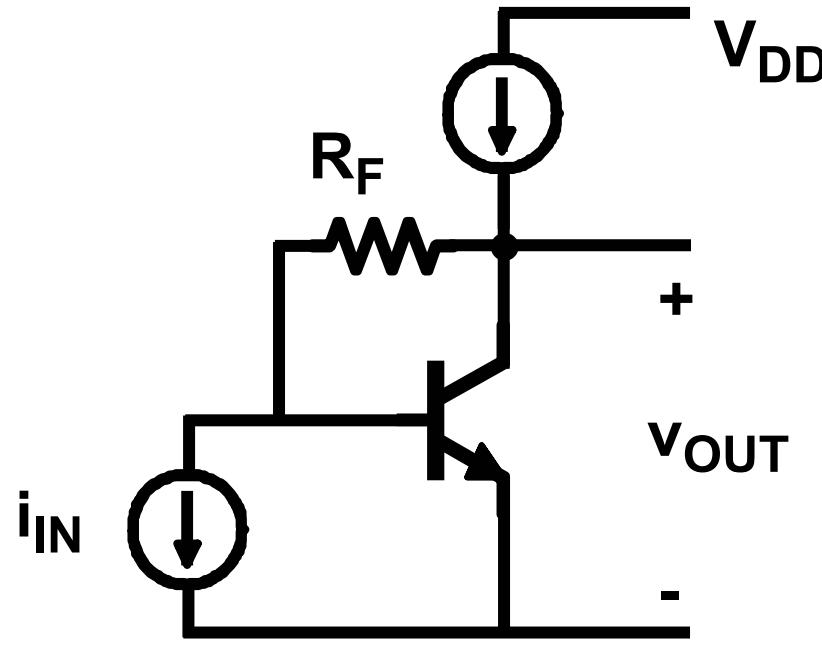
$$LG = g_m r_o$$

$$R_{IN} = \frac{R_F + r_o}{LG} \approx 0 \quad ?$$

$$R_{OUT} = \frac{r_o}{LG} \approx 0 \quad ?$$

Ref.Cherry, Proc. IEE, Feb.63, 375-389

Single bipolar transistor with shunt-shunt FB



$$A_R = R_F \quad (\text{if } >> 1/g_m)$$

$$LG = \frac{g_m r_o r_\pi}{r_o + R_F + r_\pi}$$

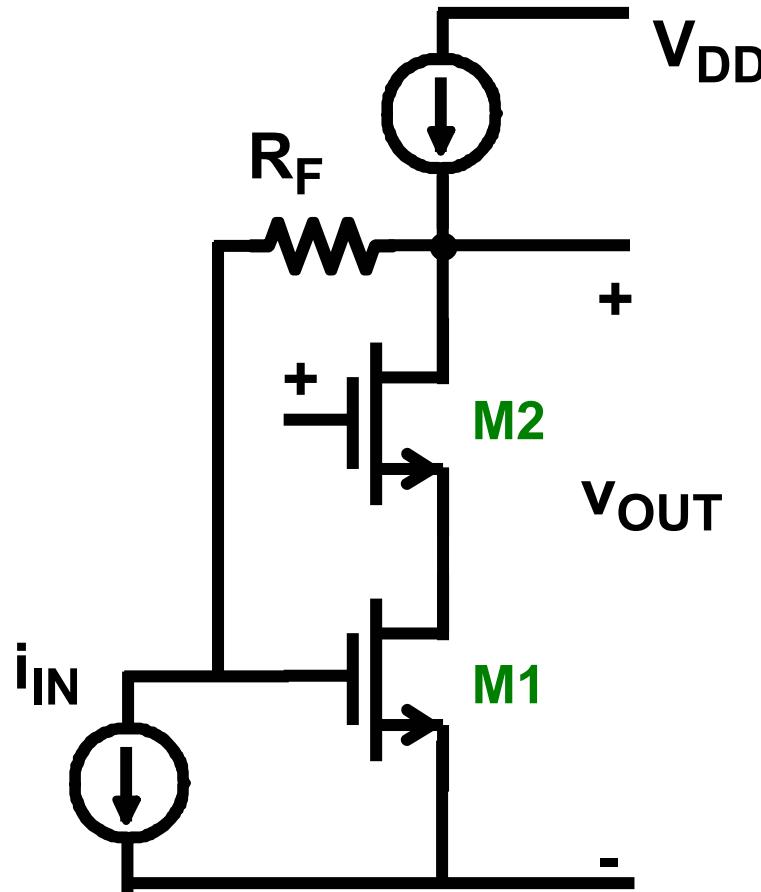
$$R_{IN} = \frac{(R_F + r_o) // r_\pi}{LG} \approx 0 ?$$

$$R_{OUT} = \frac{r_o // (R_F + r_\pi)}{LG} \approx 0 ?$$

Far from ideal !!

Output loading : $R_F + r_\pi \approx r_o$
reduces the LG !!

Cascode with shunt-shunt FB



$$A_R = R_F$$

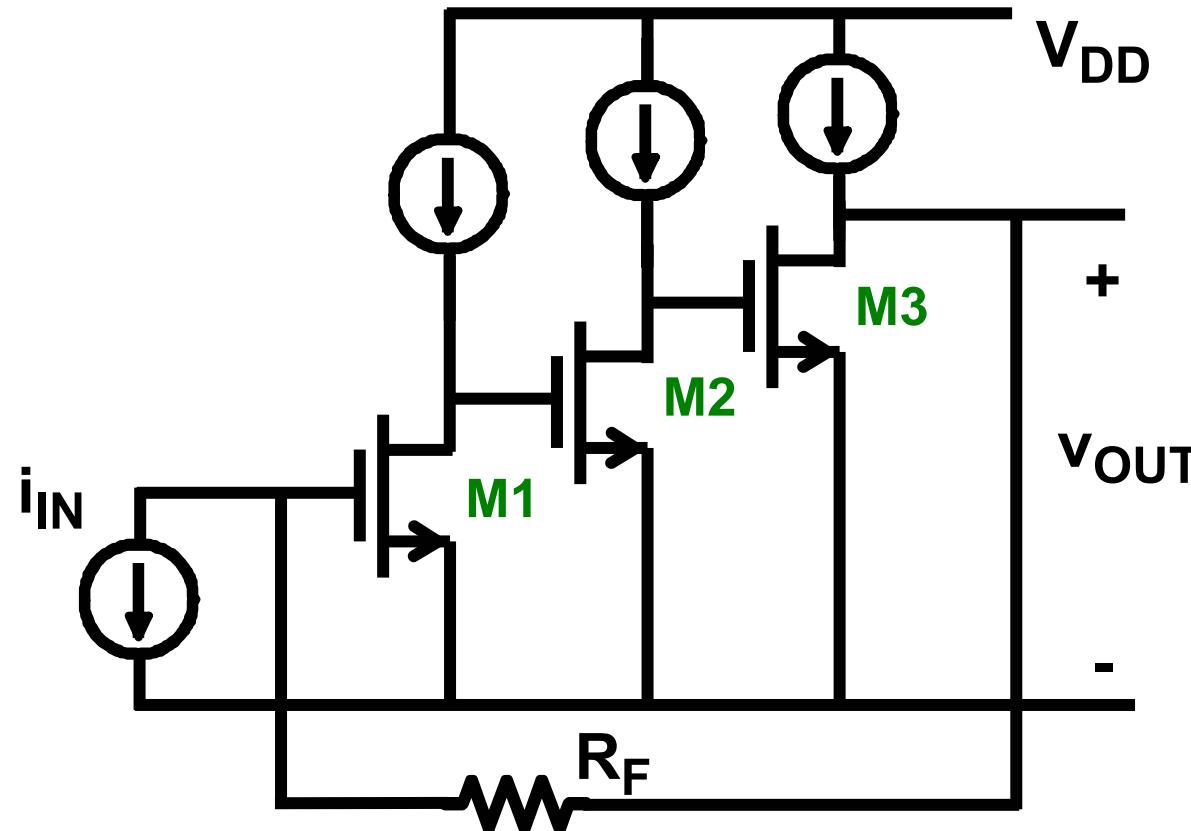
$$LG = g_{m1}r_{o1} g_{m2}r_{o2}$$

$$R_{IN} = \frac{R_F + r_{OUT}}{LG} \approx \frac{1}{g_{m1}} \approx 0$$

$$r_{OUT} = r_{o1}g_{m2}r_{o2}$$

$$R_{OUT} = \frac{r_{OUT}}{LG} \approx \frac{1}{g_{m1}} \approx 0$$

MOST Shunt-shunt FB triple



$$A_R = R_F$$

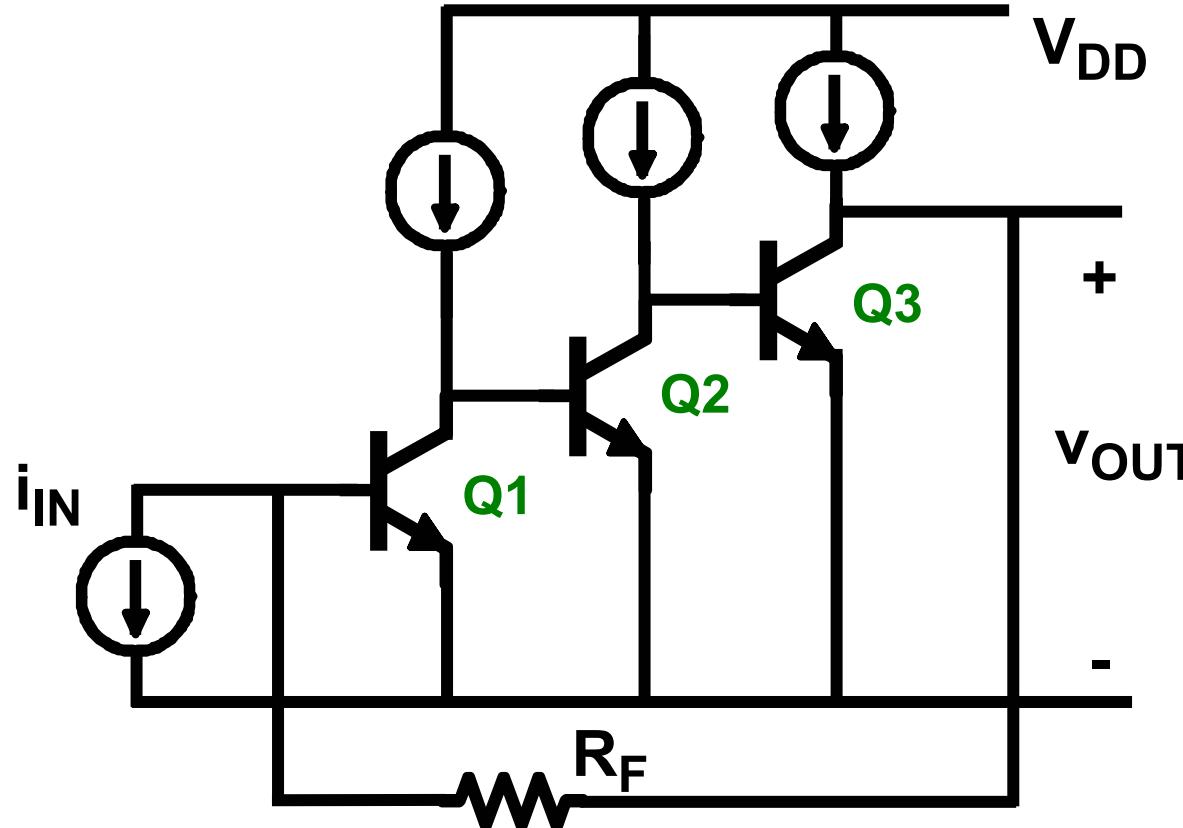
$$LG = A_{v1} A_{v2} A_{v3}$$

$$A_{vi} = g_{mi} r_{oi}$$

$$R_{IN} = \frac{R_F + r_{o3}}{LG} \approx 0$$

$$R_{OUT} = \frac{r_{o3}}{LG} \approx 0$$

Bipolar Transistor Shunt-shunt FB triple



$$A_R = R_F$$

$$LG = A_{v1} A_{v2} A_{v3}$$

$$A_{v1} = g_m 1 (r_o 1 // r_{\pi 2})$$

$$A_{v2} = g_m 2 (r_o 2 // r_{\pi 3})$$

$$A_{v3} = g_m 3 R_{OUTOL}$$

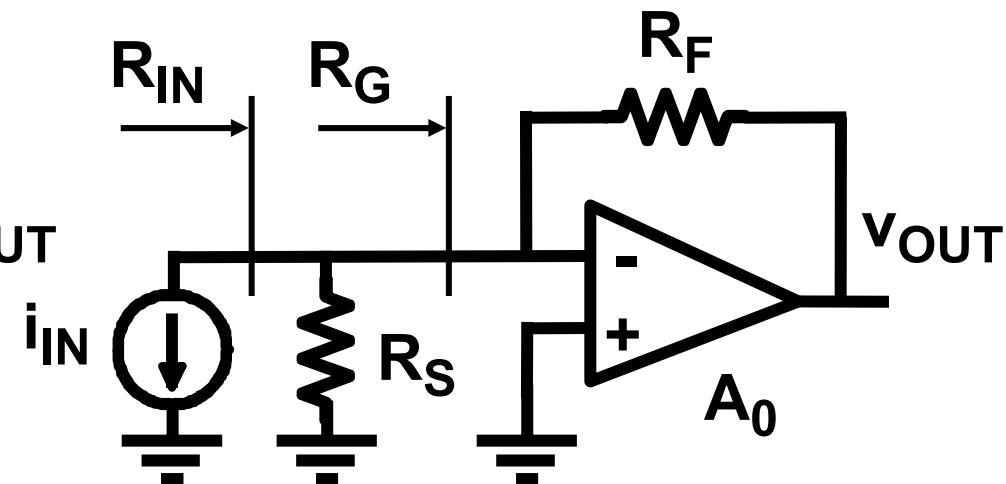
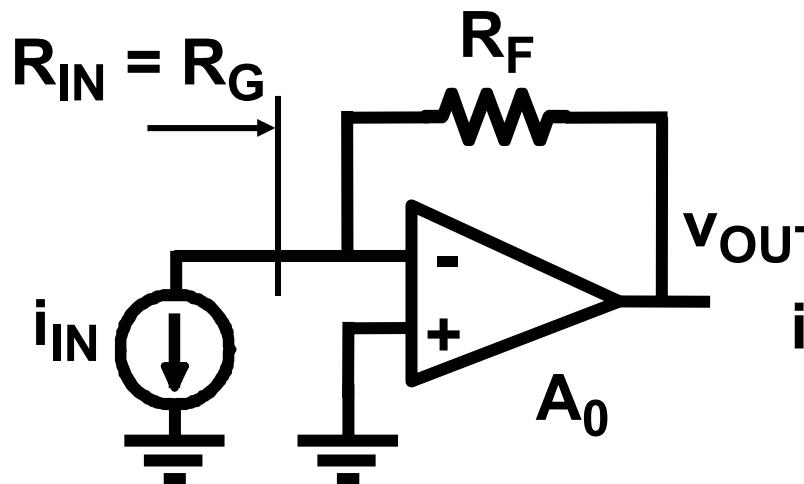
$$R_{OUTOL} = r_o 3 // (R_F + r_{\pi 1})$$

$$R_{OUT} = \frac{R_{OUTOL}}{LG} \approx 0$$

Output loading : $R_F + r_{\pi 3} \approx r_o 3$ reduces the LG !!

$$R_{IN} = \frac{(R_F + r_o 3) // r_{\pi 1}}{LG} \approx 0$$

Shunt-shunt FB with non-ideal current source



$$A_R = R_F$$

$$A_R = R_F \quad \text{if } R_S > \frac{R_F}{A_0}$$

$$LG = A_0$$

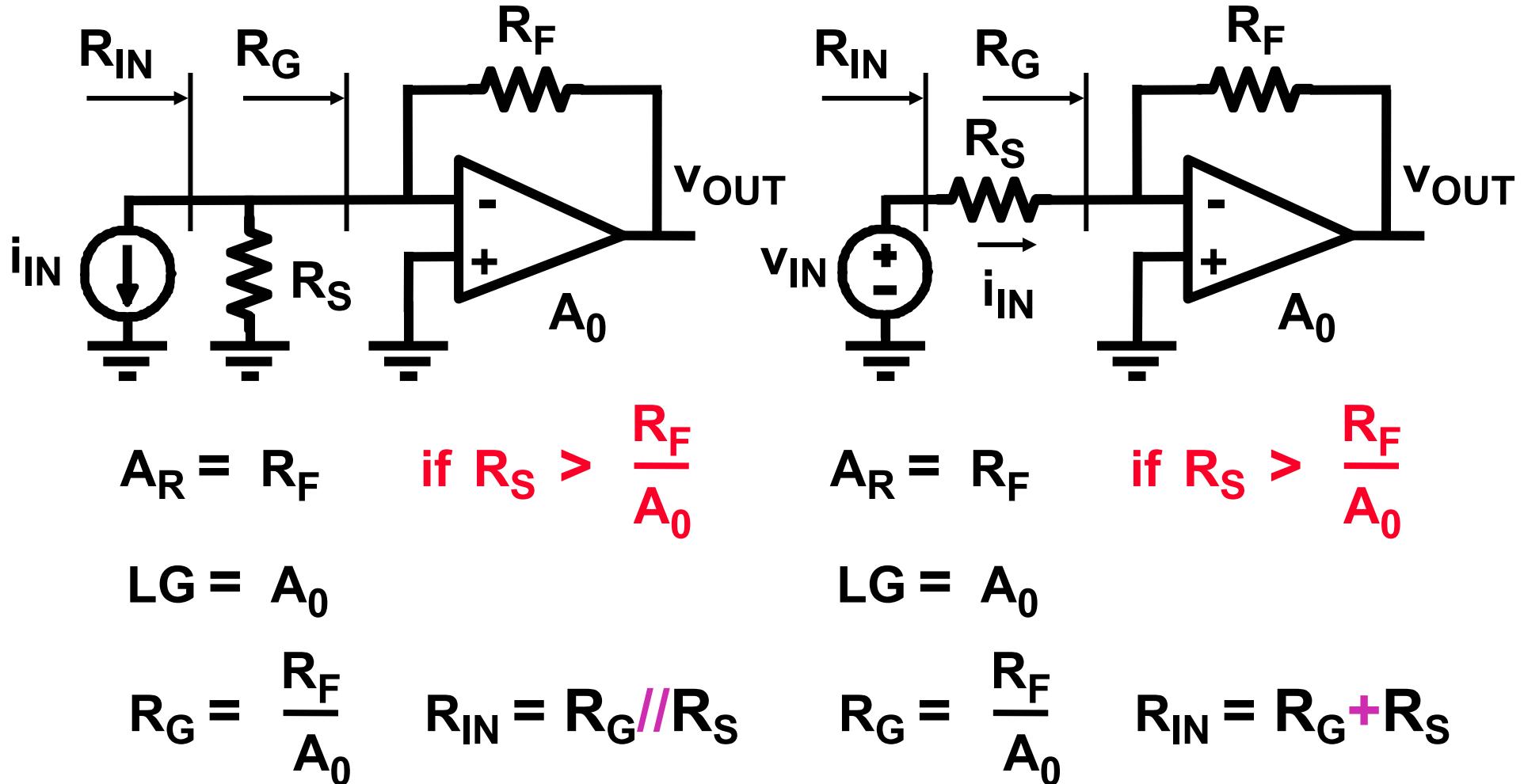
$$LG = A_0$$

$$R_{IN} = \frac{R_F}{A_0}$$

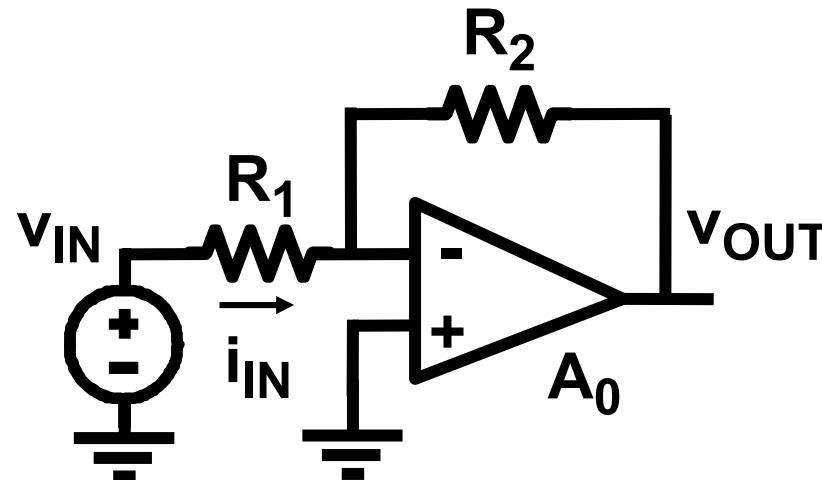
$$R_G = \frac{R_F}{A_0}$$

$$R_{IN} = R_G // R_S$$

Shunt-shunt FB with voltage source



Shunt-shunt feedback : Gain and R_{OUT}



$$LG = A_0 \quad A_0 \approx 10^4 \dots 10^6$$

$$A_R = R_2 \quad \text{if } R_1 > \frac{R_2}{A_0}$$

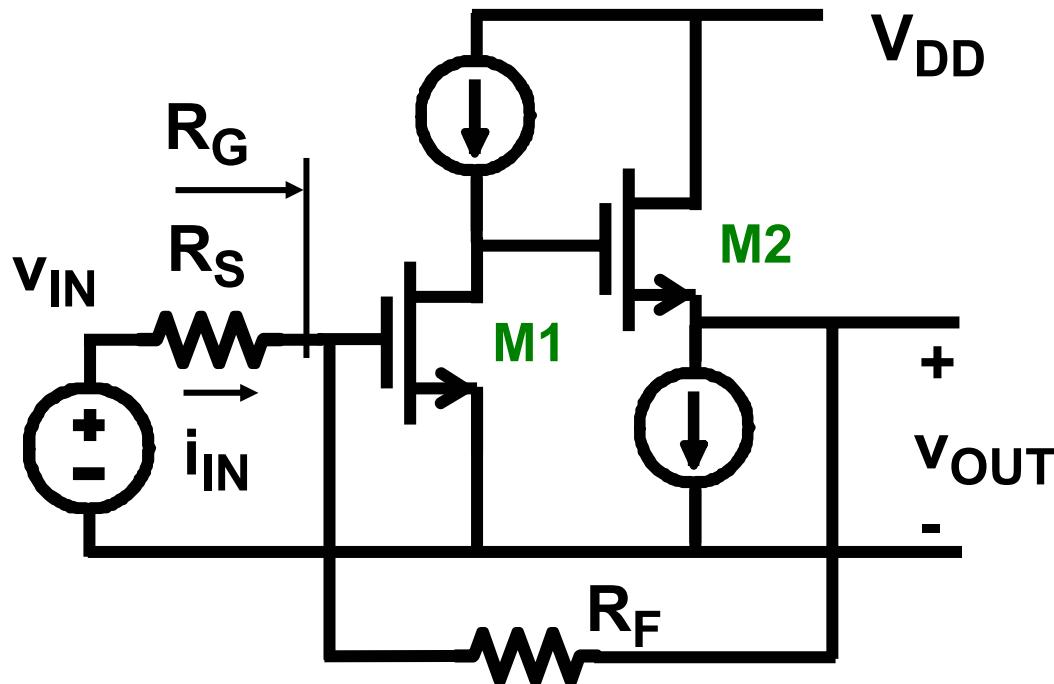
$$\frac{v_{\text{OUT}}}{v_{\text{IN}}} = \frac{v_{\text{OUT}}}{i_{\text{IN}}} \frac{i_{\text{IN}}}{v_{\text{IN}}}$$

$$A_v = -A_R \frac{1}{R_1}$$

$$A_v = -\frac{R_2}{R_1}$$

$$R_{\text{OUT}} = \frac{R_{\text{OUTOL}}}{LG}$$

Shunt-shunt FB pair with voltage source



$$A_R = R_F \quad A_v = -\frac{R_F}{R_S}$$

$$LG = g_{m1}r_{o1}$$

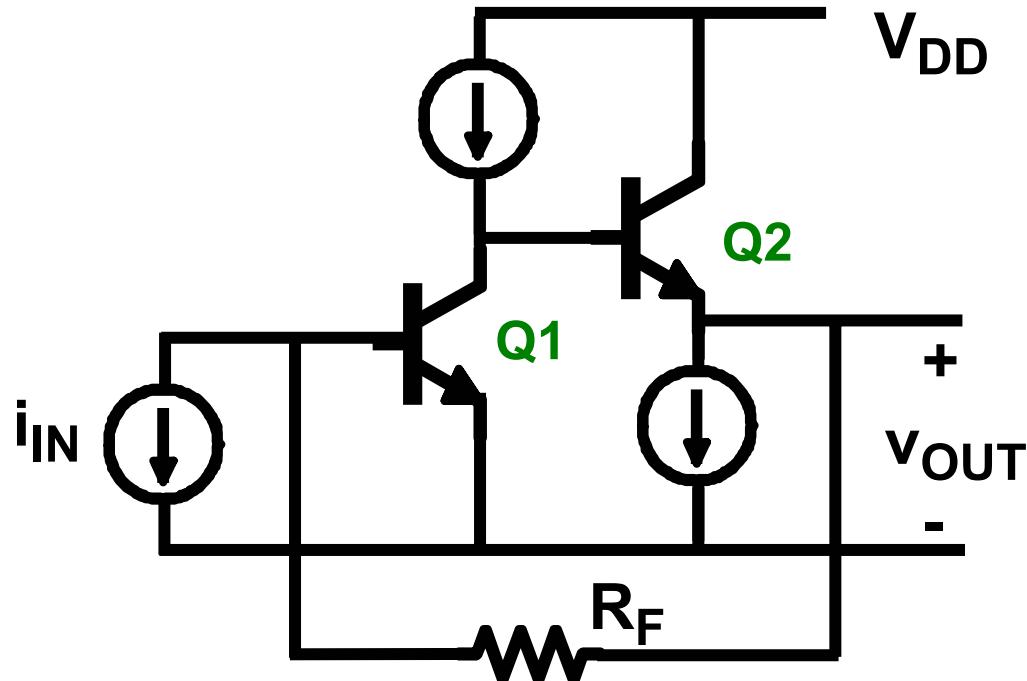
$$R_{IN} = R_S + R_G$$

$$R_G = \frac{R_F}{LG} = \frac{R_F}{g_{m1}r_{o1}} \approx 0$$

if $R_S > \frac{R_F}{A_0}$

$$R_{OUT} = \frac{1/g_{m2}}{LG} \approx 0$$

Shunt-shunt FB pair with input loading



$$A_R = R_F$$

$$LG = g_{m1} r_{o1} \frac{r_{\pi1}}{R_F + r_{\pi1}}$$

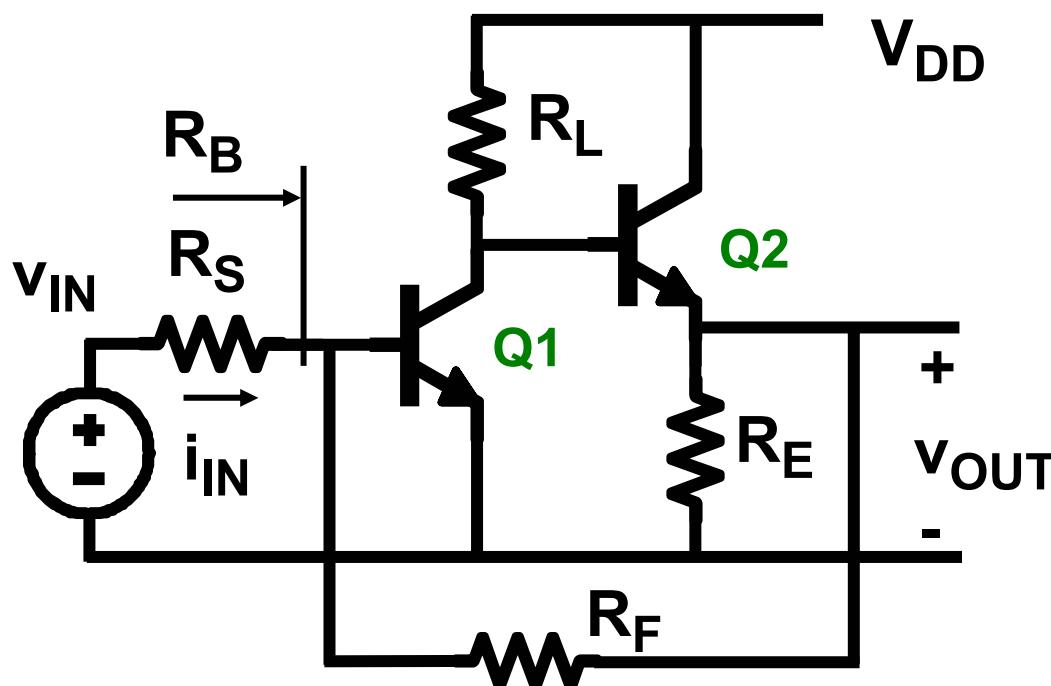
$$R_{IN} = \frac{R_F // r_{\pi1}}{LG} = \frac{R_F}{g_{m1} r_{o1}} \approx 0$$

$$R_{OUT} = \frac{R_{OUTOL}}{LG} \approx 0$$

$$R_{OUTOL} = \frac{1}{g_{m2}} + \frac{r_{o1}}{\beta}$$

Input loading : $R_F \approx r_{\pi1}$

Shunt-shunt FB pair with voltage source



$$A_R = -R_F \quad A_v = -\frac{R_F}{R_S}$$

$$LG = g_m R_L \frac{r_{\pi 1}}{R_F + r_{\pi 1}}$$

$$R_B = \frac{R_F // r_{\pi 1}}{LG} \approx 0$$

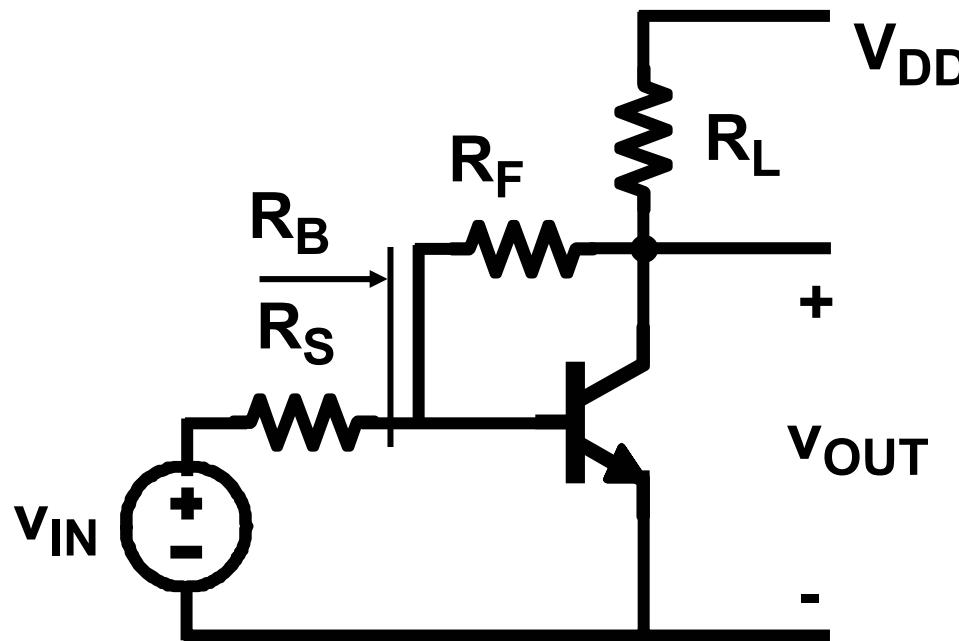
$$R_{IN} = R_S + R_B$$

Input loading :

$$R_F \approx r_{\pi 1}$$

$$R_{OUT} = \frac{R_{OUTOL}}{LG} \approx 0 \quad R_{OUTOL} = \frac{1}{g_{m2}} + \frac{R_L}{\beta}$$

Non-ideal single-transistor shunt-shunt FB



$$A_R \approx R_F \quad A_v \approx -\frac{R_F}{R_S}$$

$$LG \approx g_m r_o L F$$

$$R_{IN} = R_S + R_B$$

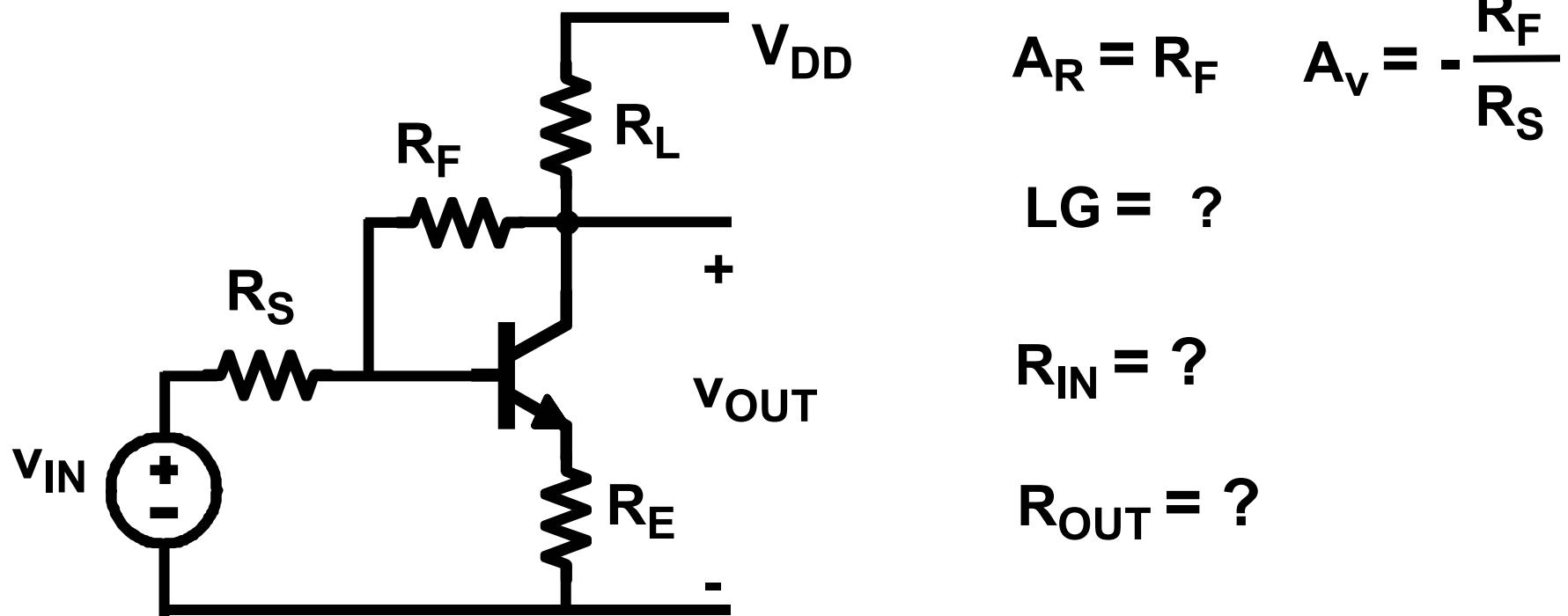
$$R_B \approx \frac{r_\pi // (R_F + r_{oL})}{LG} \approx 0$$

$$R_{OUT} \approx \frac{r_{oLF}}{LG} \approx 0 \text{ ??}$$

Output loading : $R_F \approx r_{oL}$ $r_{oL} = r_o // R_L$ $r_{oLF} = r_o // R_L // R_F$

Input loading : $R_F \approx r_\pi$

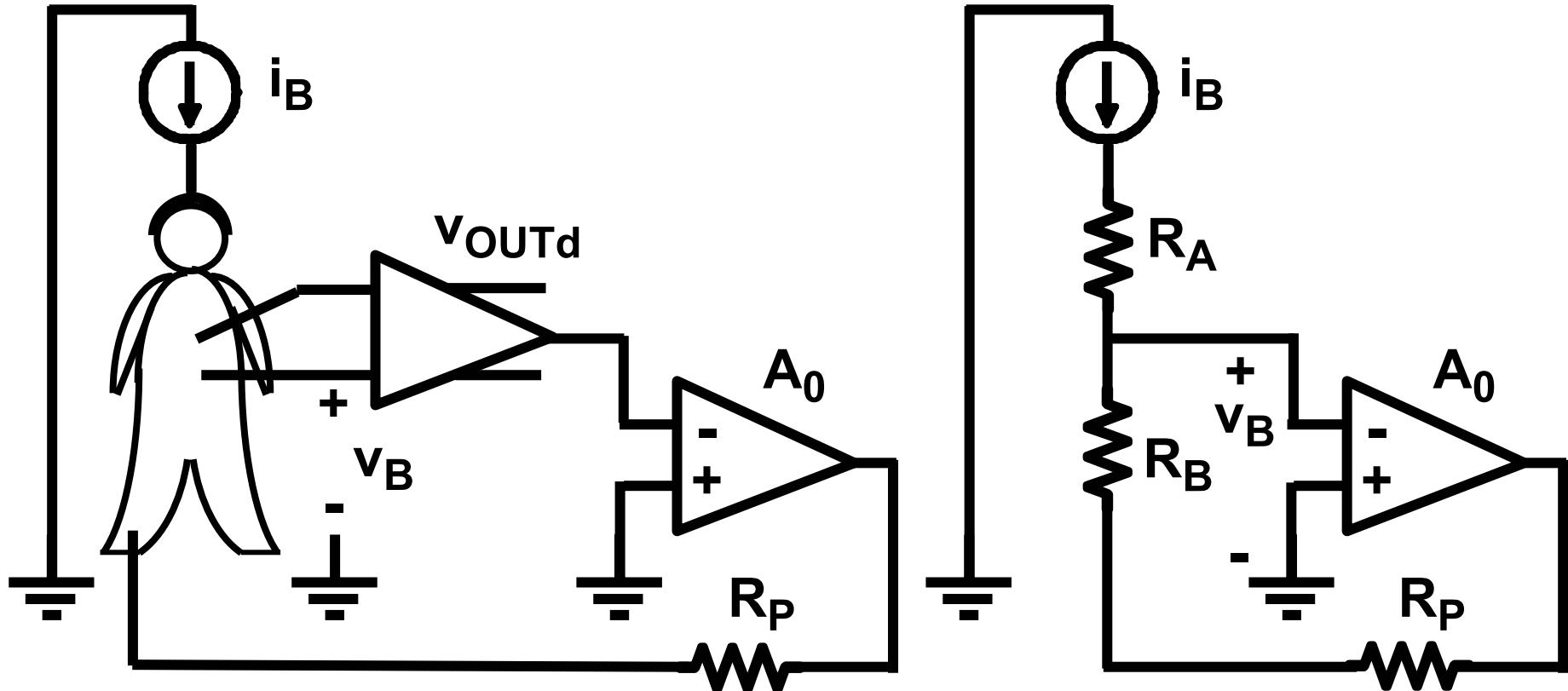
Non-ideal single-transistor Feedback



Output loading : $R_F \approx r_{oL}$ $r_{oL} = r_o // R_L$

Input loading : $R_F \approx r_\pi$

Shunt-shunt feedback in Right-leg drive



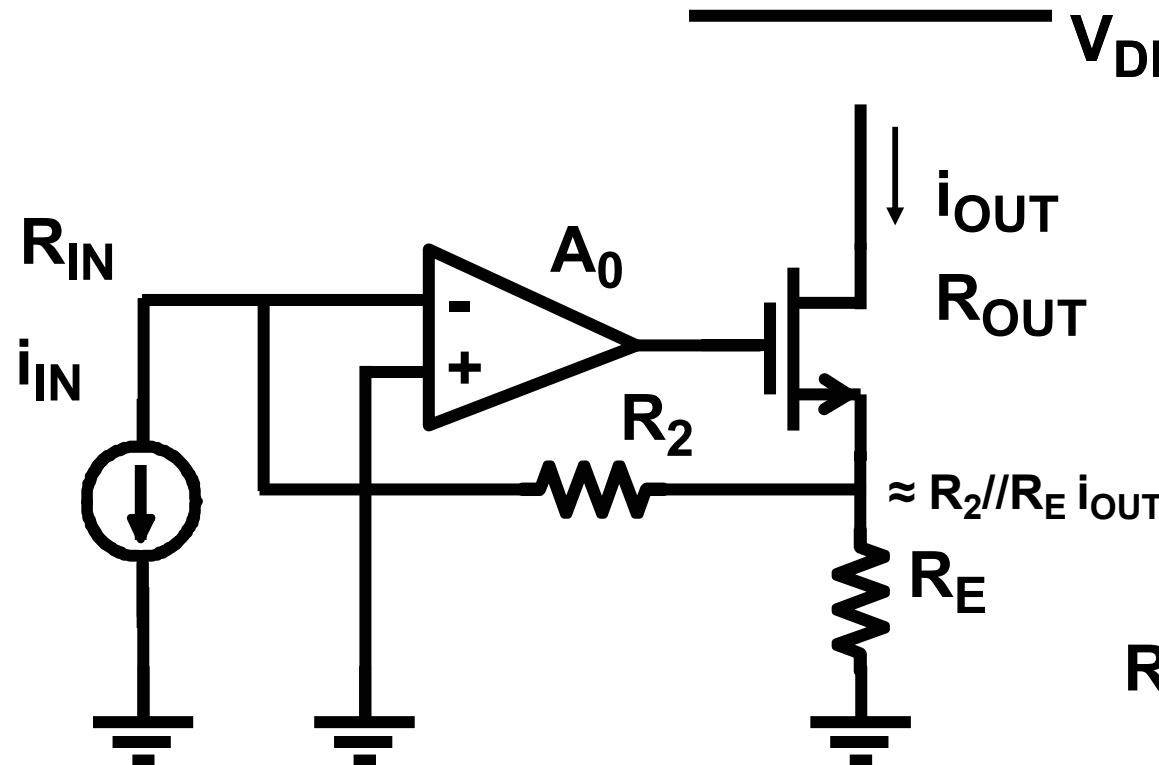
$i_B \approx 10 \mu\text{A}_{\text{RMS}}$
for $220 \text{ V}_{\text{RMS}}$ (50 Hz) through 150 pF

$$\frac{v_B}{i_B} = \frac{R_P + R_B}{A_0 + 1}$$

Table of contents

- Introduction
- Shunt-shunt FB for Transimpedance amps.
- Shunt-series FB for current amplifiers
- Transimpedance amplifiers for
low noise and high frequencies

Shunt-series feedback : Gain, R_{IN} & R_{OUT}



$$LG = A_0$$

$$A_I = 1 + \frac{R_2}{R_E}$$

$$R_{IN} = \frac{R_2^*}{LG} \approx 0$$

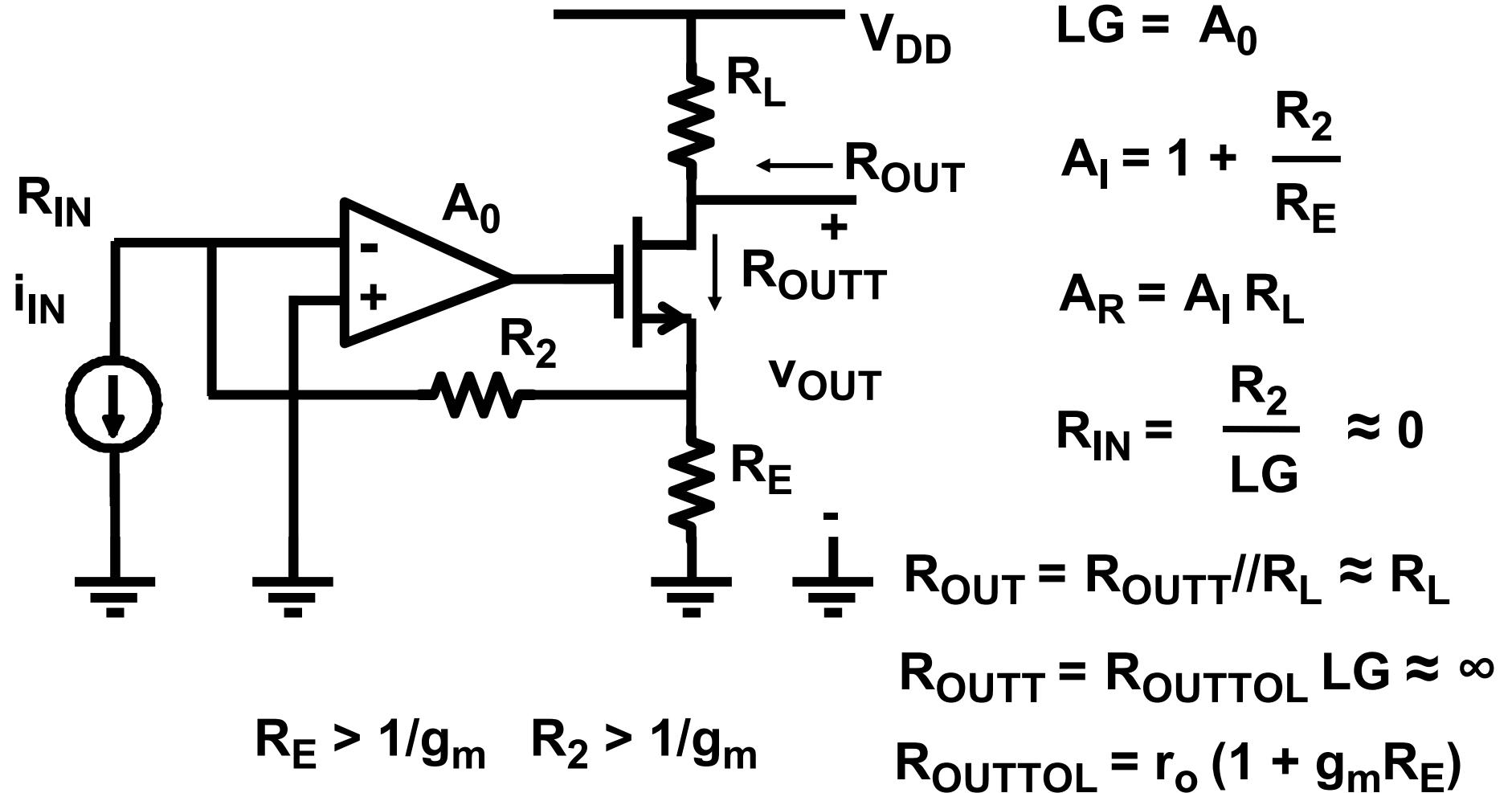
$$R_{OUTOL} = r_o (1 + g_m R_E)$$

$$R_{OUT} = R_{OUTOL} \quad LG \approx \infty$$

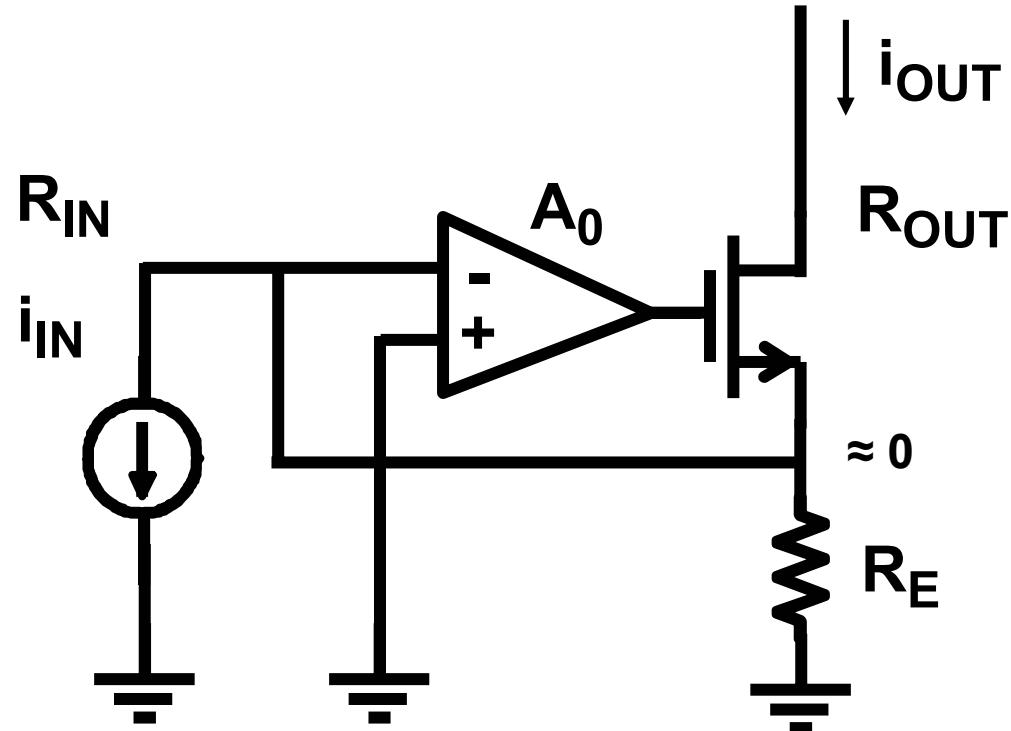
$$R_E > 1/g_m \quad R_2 > 1/g_m$$

$$R_2^* = R_2 + R_E/(1+g_m R_E) \approx R_2$$

Shunt-series feedback with load R_L



Ideal current buffer



$$A_I = 1$$

$$LG = A_0$$

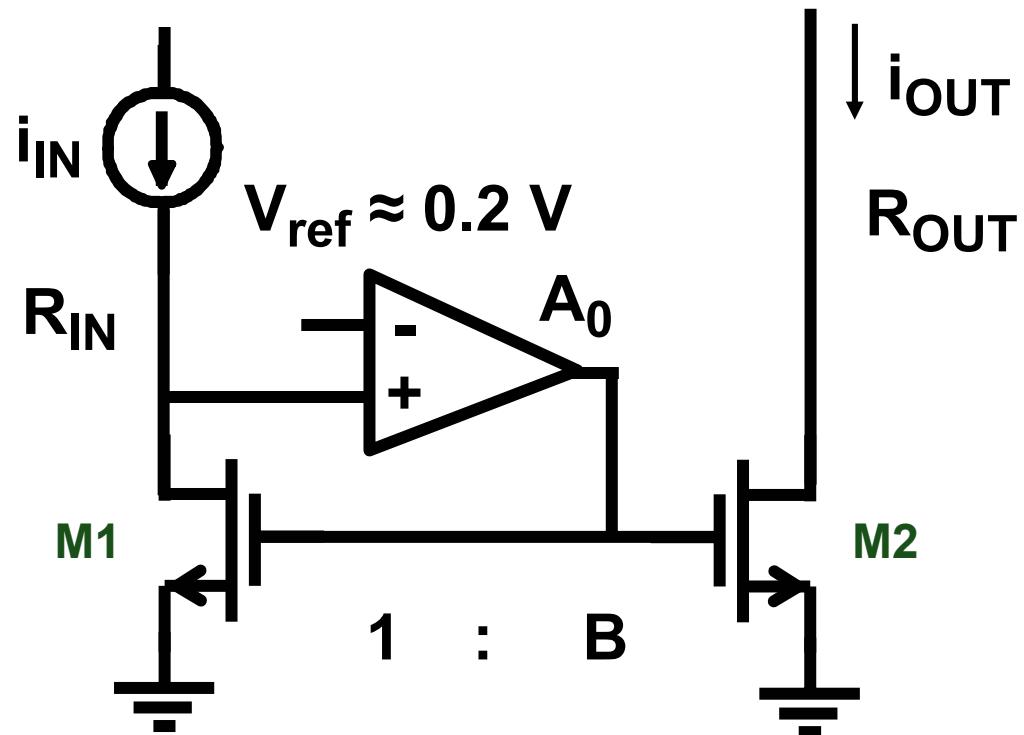
$$R_{IN} = \frac{1/g_m}{LG} \approx 0$$

$$R_{OUTOL} = r_o (1 + g_m R_E)$$

$$R_E > 1/g_m$$

$$R_{OUT} = R_{OUTOL} \quad LG \approx \infty$$

Ideal current mirror



$$i_{OUT} = B i_{IN} \quad A_I = B$$

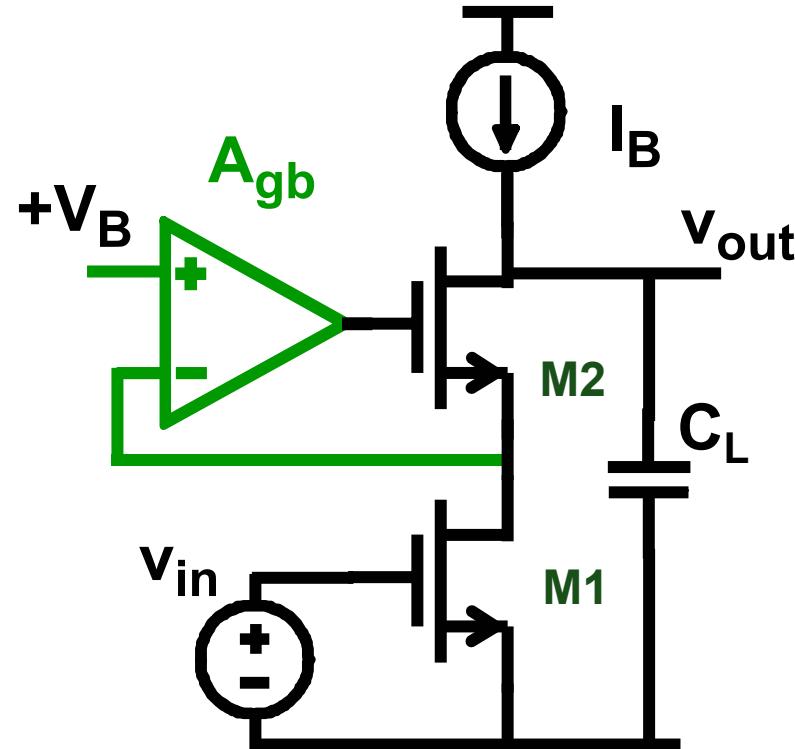
$$LG = g_m r_o A_0$$

$$R_{IN} = \frac{R_{INOL}}{LG} = \frac{1}{g_m A_0} \approx 0$$

$$R_{INOL} = r_o$$

$$R_{OUT} = r_o$$

Gain boosting



$$A_v = A_{gb} (g_m r_{DS})_1 (g_m r_{DS})_2$$

Hosticka, JSSC Dec.79, pp. 1111-1114; Sackinger, JSSC Febr.90, pp. 289-298;
Bult JSSC Dec.90, pp. 1379-1384

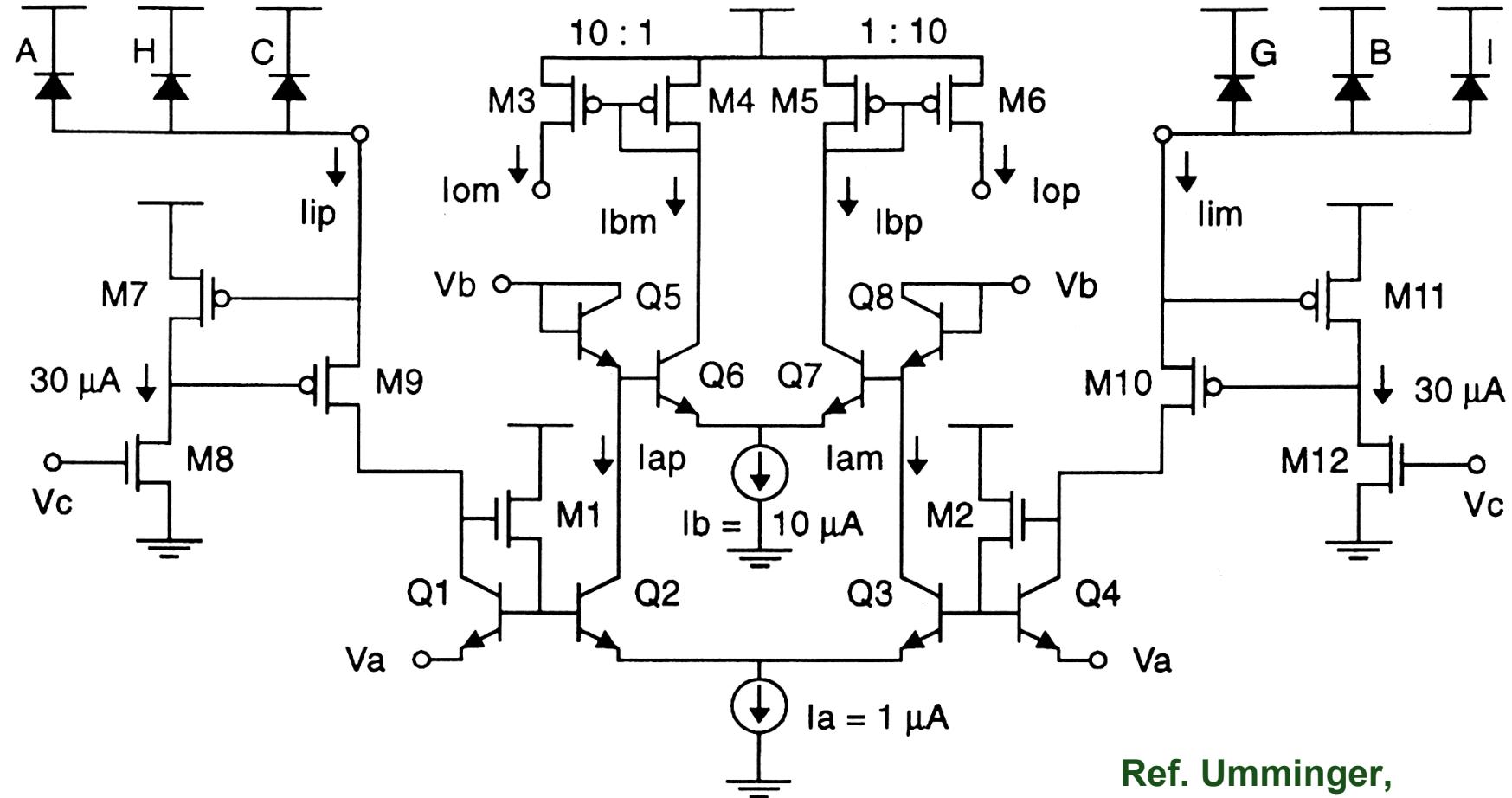
$$LG = A_{gb}$$

$$R_{E2} = \frac{1/g_{m2}}{LG} \approx 0$$

$$R_{OUTOL} = r_{o2} (1 + g_{m2} r_{o1})$$

$$R_{OUT} = R_{OUTOL} LG \approx \infty$$

Differential current amplifier



Ref. Umminger,
JSSC Dec.95, 1382-1390

Linear laser diode driver

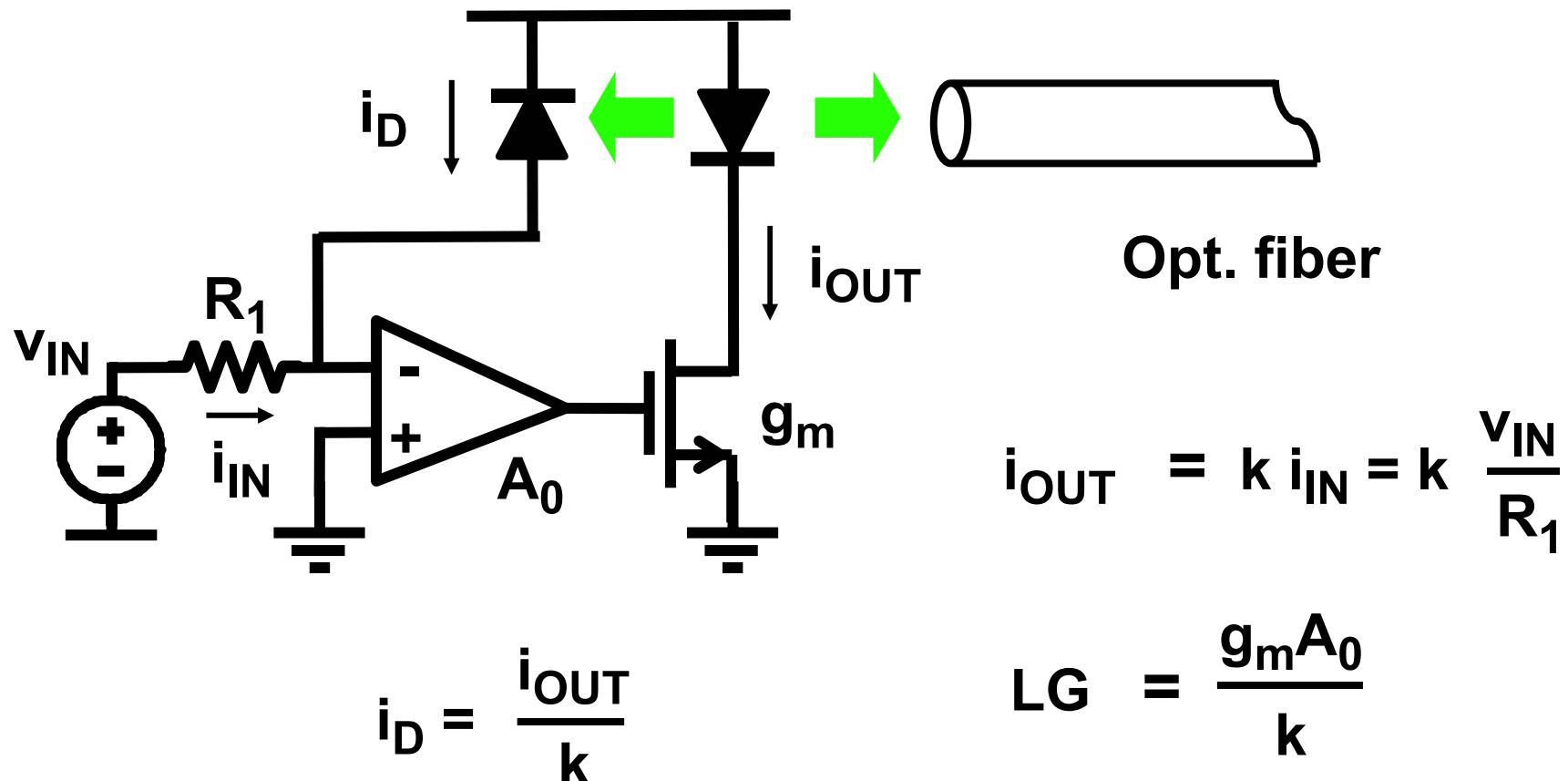
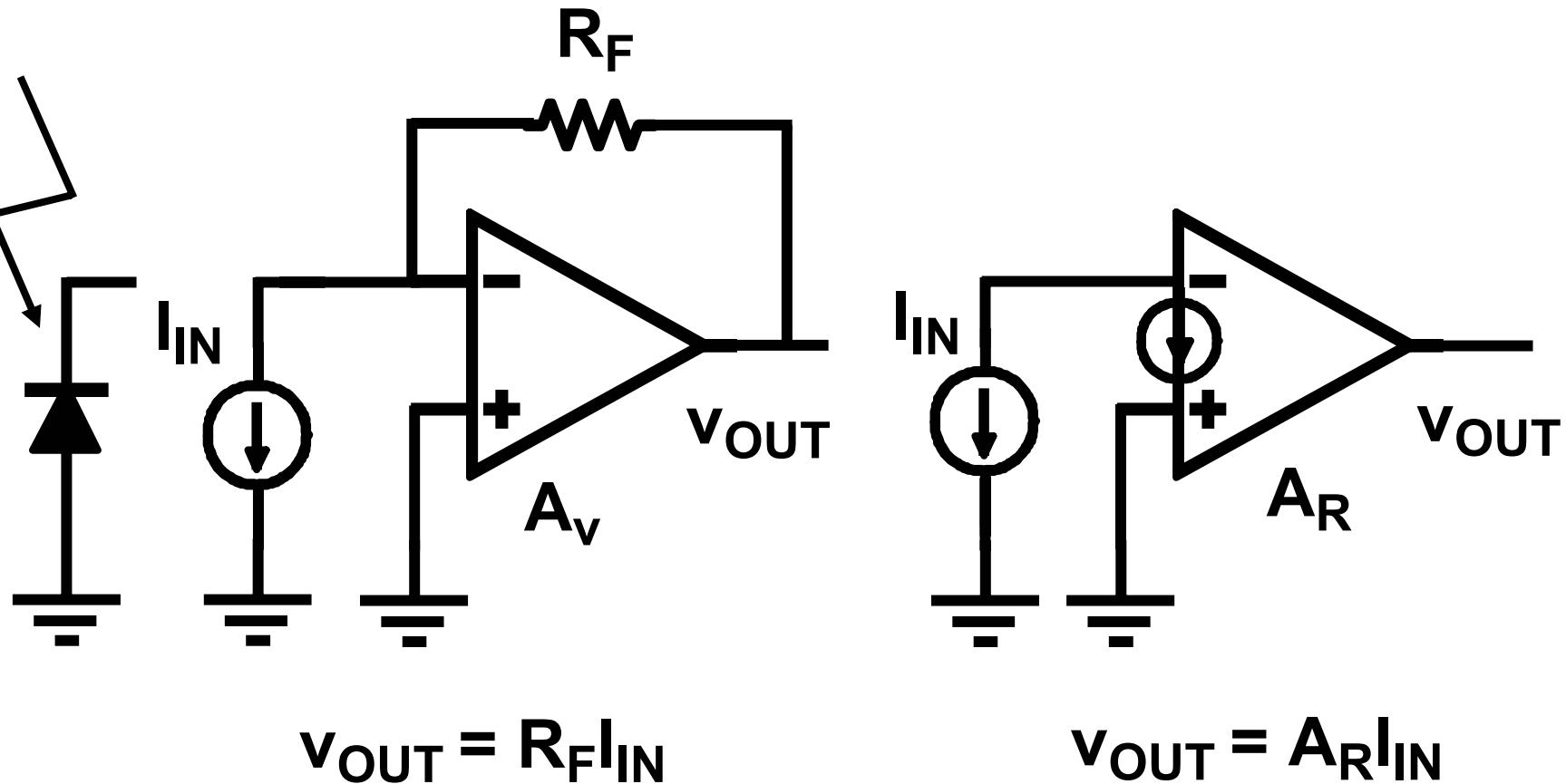


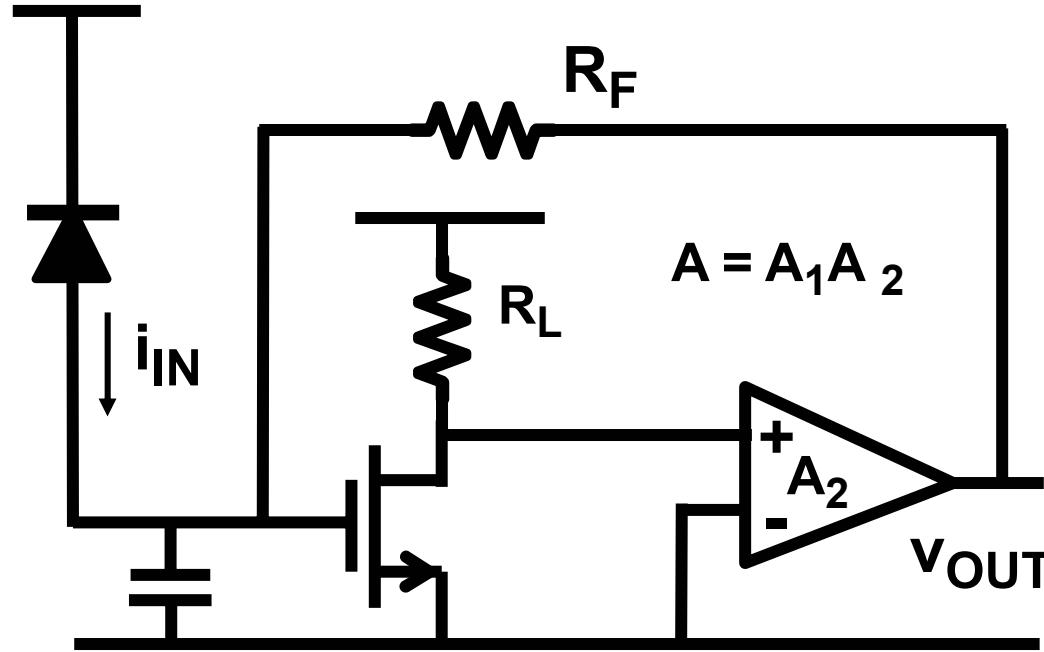
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- Introduction
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Optical receiver : Current or voltage amplifier



Current detector with voltage amplifier



$$C_P = C_D + C_{GS} \quad A_1 = g_m R_L$$

Noise matching : $C_D = C_{GS}$

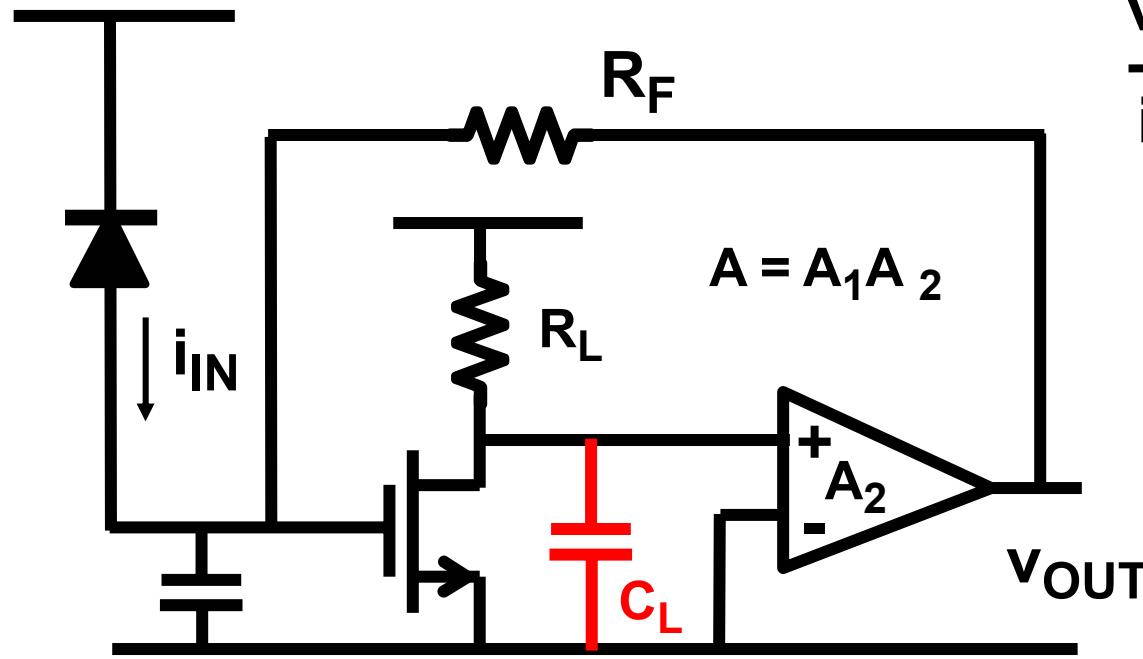
$$\frac{V_{IN}}{i_{IN}} = \frac{R_F}{A_1 A_2} \frac{1}{1 + R_F \frac{C_P}{A_1 A_2} s}$$

$$\frac{V_{OUT}}{i_{IN}} = R_F \frac{1}{1 + R_F \frac{C_P}{A_1 A_2} s}$$

$$T = \frac{A_1 A_2}{1 + R_F C_P s}$$

$$A_R \text{ BW } (\text{THz}\Omega) = \frac{A_1 A_2}{2\pi C_P}$$

Current detector with voltage amplifier



$$\frac{v_{IN}}{i_{IN}} = \frac{R_F}{A_1 A_2} \frac{1 + R_L C_L s}{1 + as + bs^2}$$

$$a = \frac{R_F C_P}{A_1 A_2}$$

$$b = \frac{R_F C_P R_L C_L}{A_1 A_2}$$

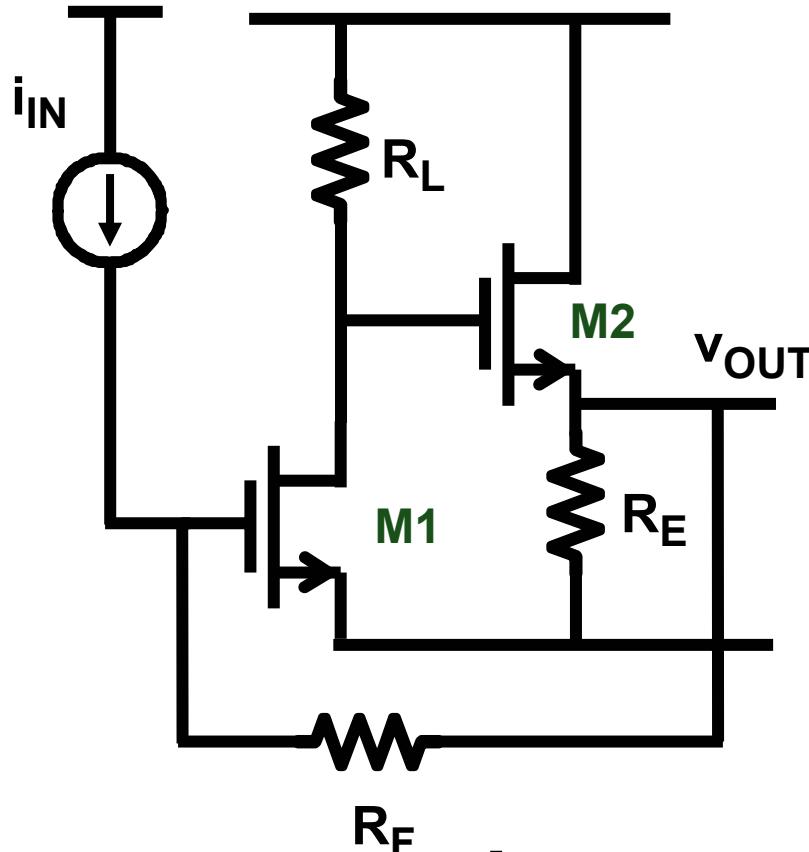
$$C_P = C_D + C_{GS}$$

$$A_1 = g_m R_L$$

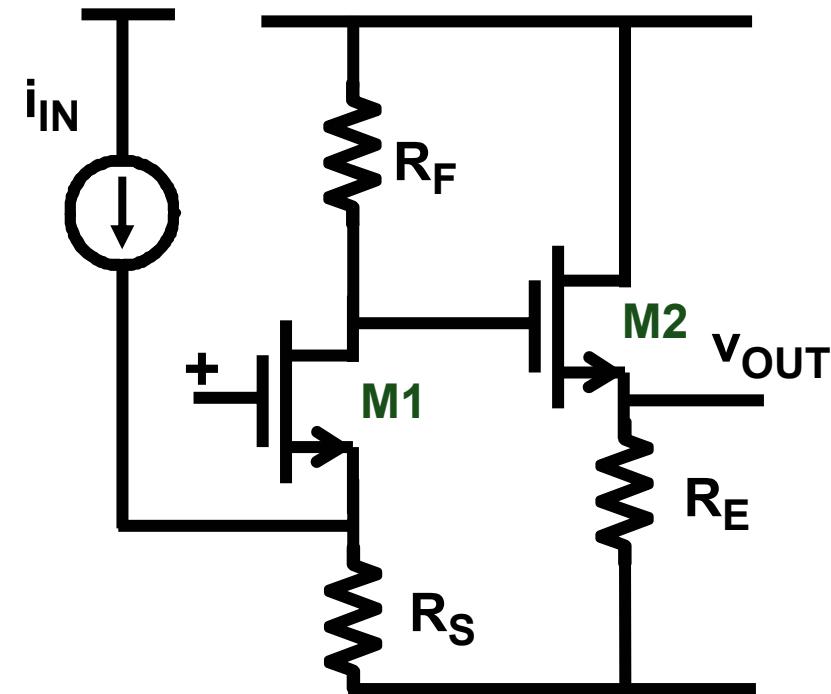
No peaking if $R_L < \sqrt{\frac{R_F}{4g_m A_2}} \frac{C_P}{C_L}$

$$\frac{v_{OUT}}{i_{IN}} = R_F \frac{1}{1 + as + bs^2}$$

BW in voltage/current amplifier



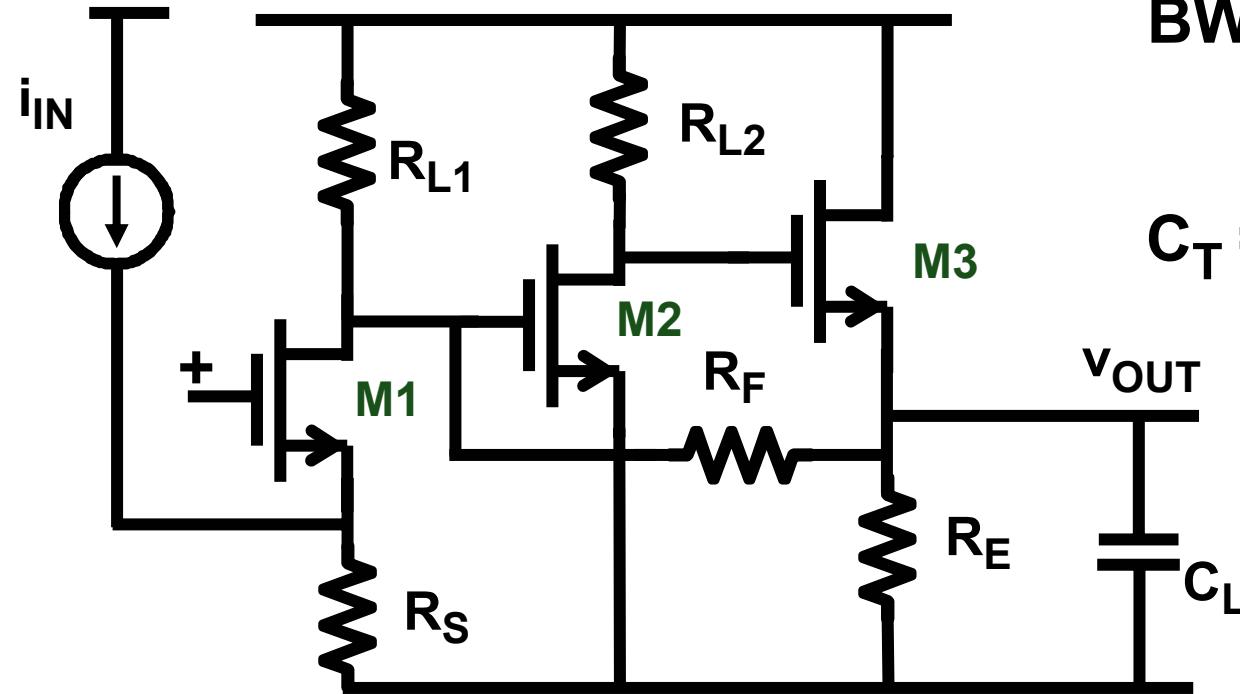
$$BW = \frac{A_{v1}}{2\pi R_F(C_{GS1} + C_D)}$$



$$R_S \gg 1/g_{m1}$$

$$BW = \frac{1}{2\pi R_F(C_{GD2} + C_{DB1})}$$

Current detector with input cascode



$$BW = \frac{A_{v2}}{2\pi R_F // R_{L1} C_T}$$

$$C_T = C_{GS2} + A_{v2} C_{GD2}$$

$$A_{v2} = g_{m2} R_{L2}$$

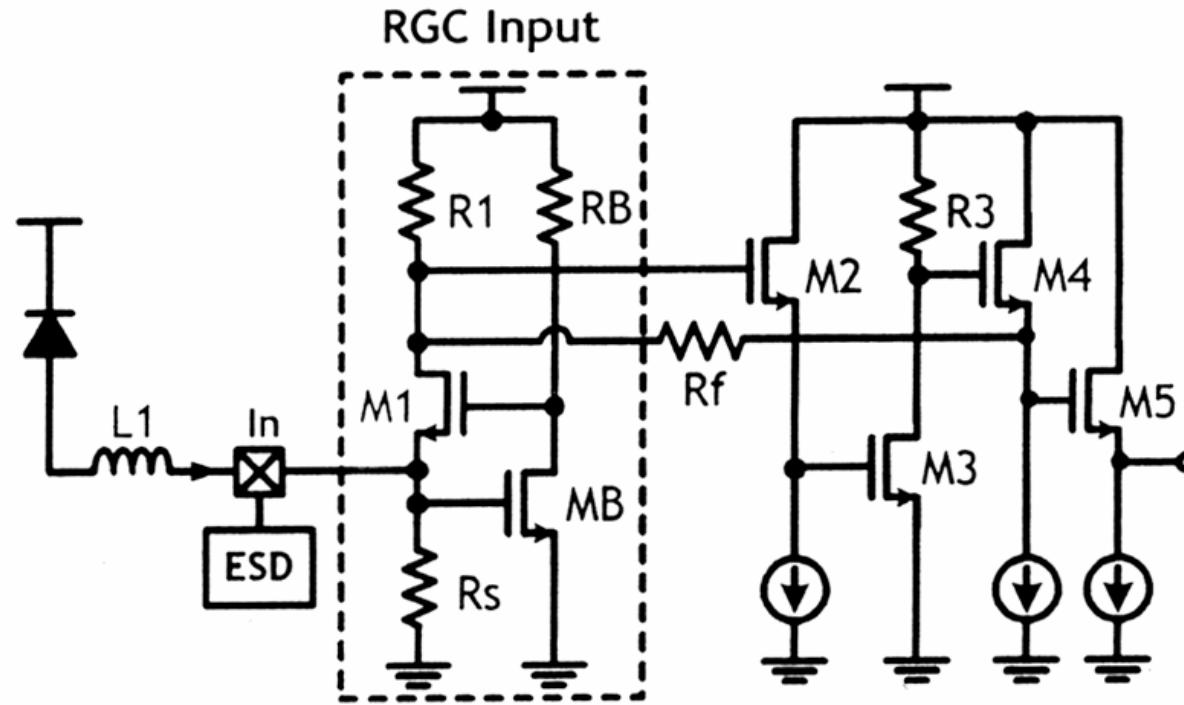
$$V_{OUT} = R_F i_{IN}$$

$$R_{OUT} = \frac{1/g_{m3}}{A_{v2}}$$

Z_{IN} independent of f ! $R_S \gg 1/g_{m1}$

Vanisri, et al, JSSC June 95, pp. 677-685

Current detector with regulated cascode



5 V 17 mA

$C_D = 0.5 \text{ pF}$

$R_F = 800 \Omega$

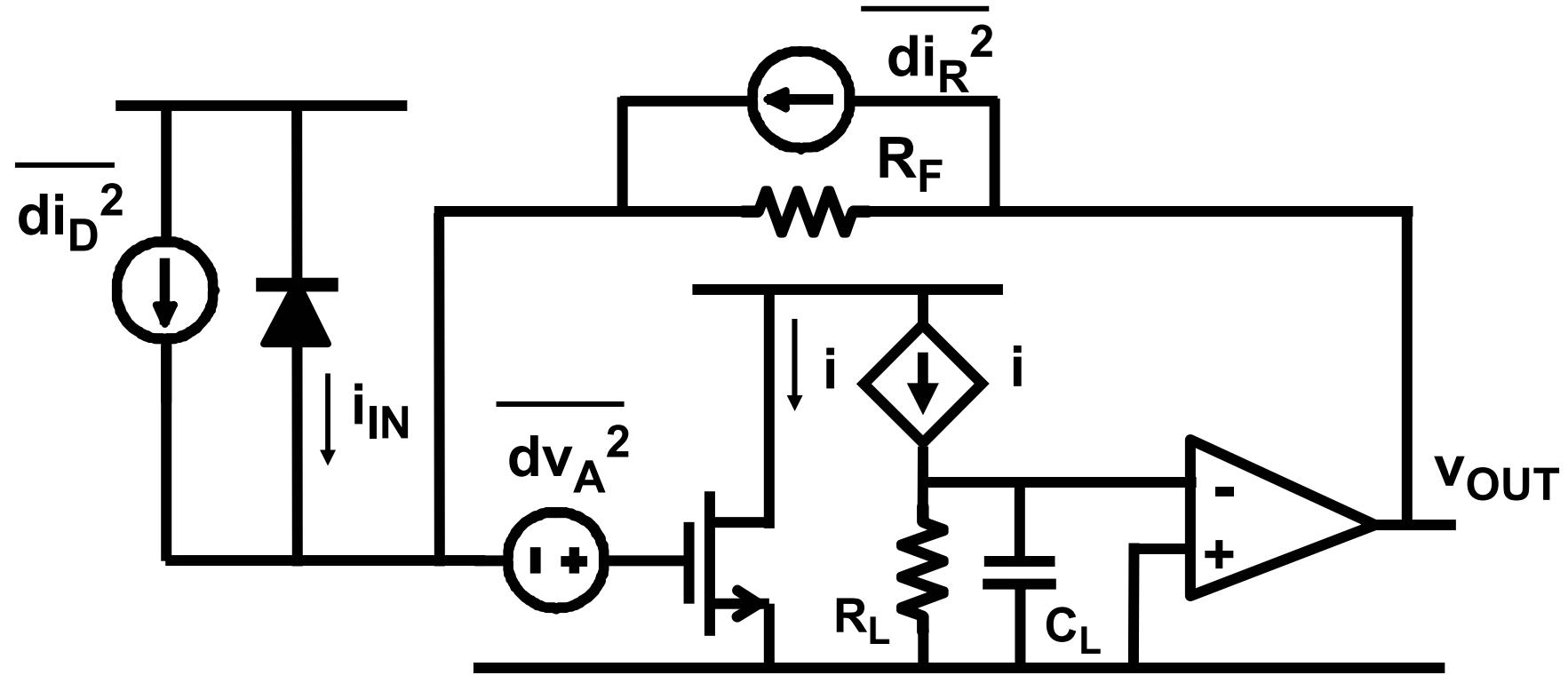
$\text{BW} = 1 \text{ GHz}$

$g_{mB} = 3 g_{m1}$

BW independent of C_D ! Current noise : R_s & $R_F // R_1$

Park, JSSC Jan. 04, 112-120

Noise sources of detector voltage amplifier

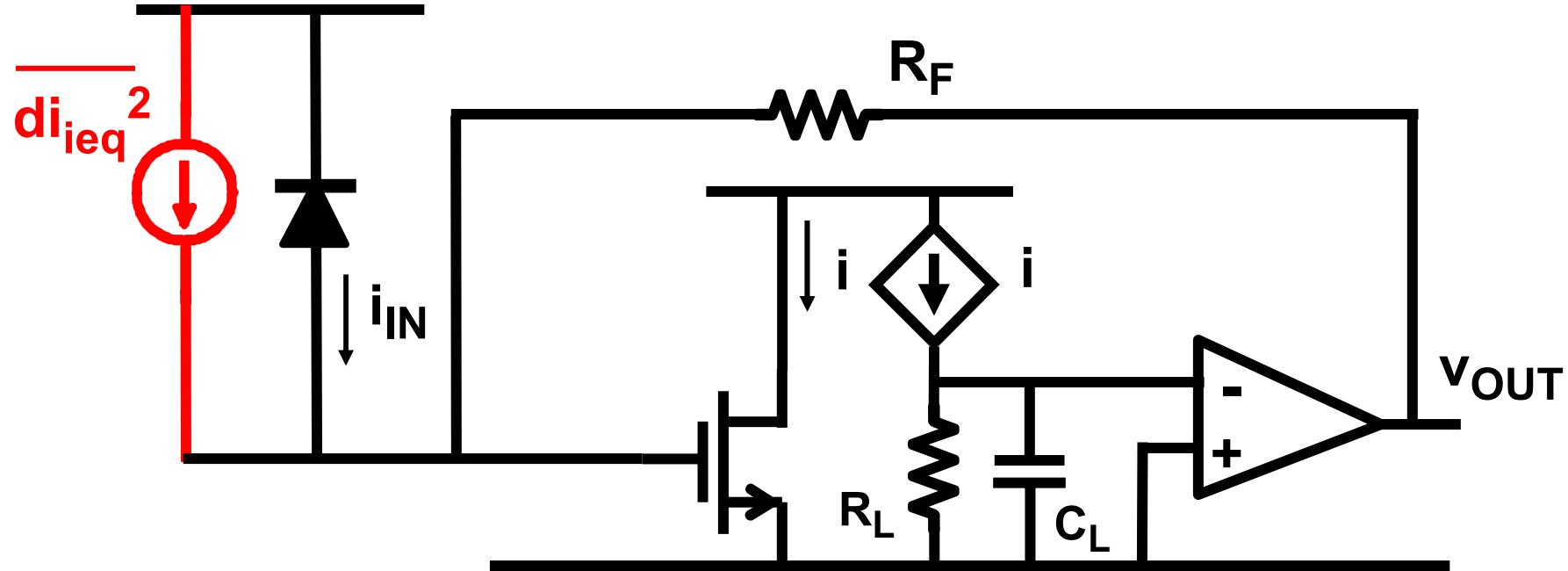


$$\overline{di_D^2} = 2qI_D df$$

$$\overline{di_R^2} = \frac{4kT}{R_F} df$$

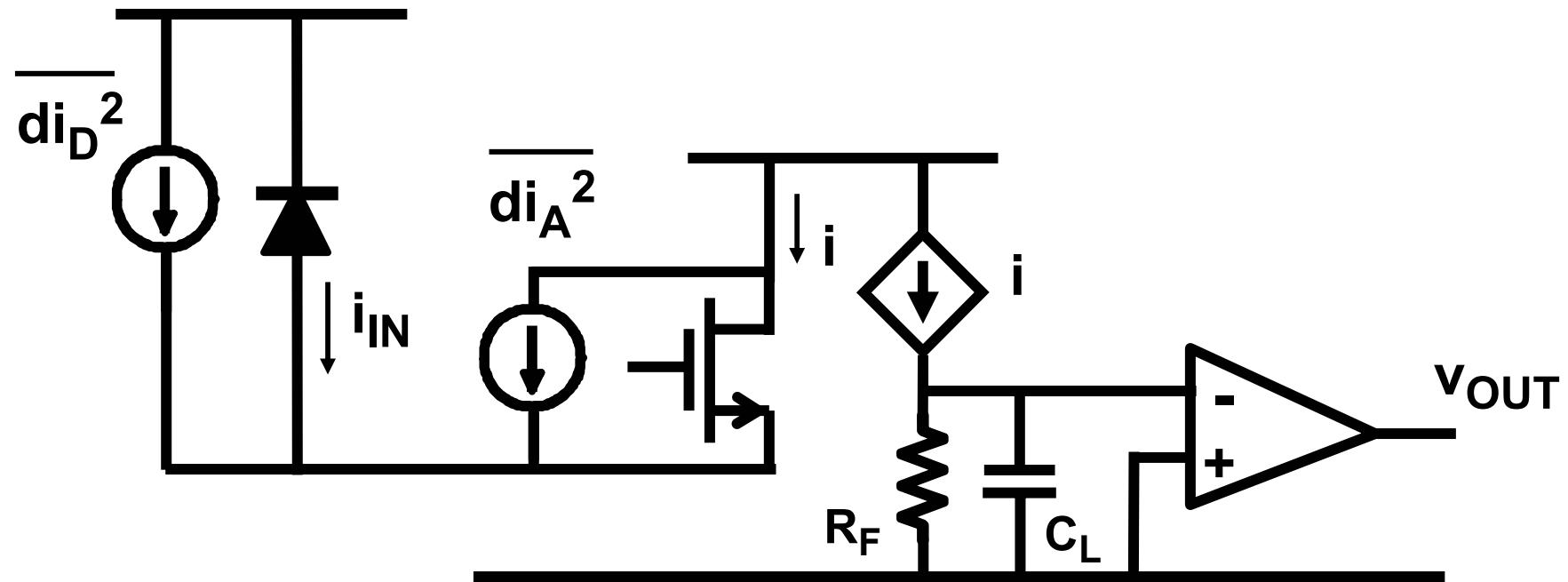
$$\overline{dv_A^2} = 4kT \left(\frac{2/3}{g_m} \right) df$$

Noise density of detector voltage amplifier



$$\overline{di_{ieq}^2} = \overline{di_D^2} + \overline{di_R^2} + \frac{\overline{dv_A^2}}{R_F^2} \approx \overline{di_D^2} + \overline{di_R^2} \quad \text{if } R_F > \frac{2/3}{g_m}$$

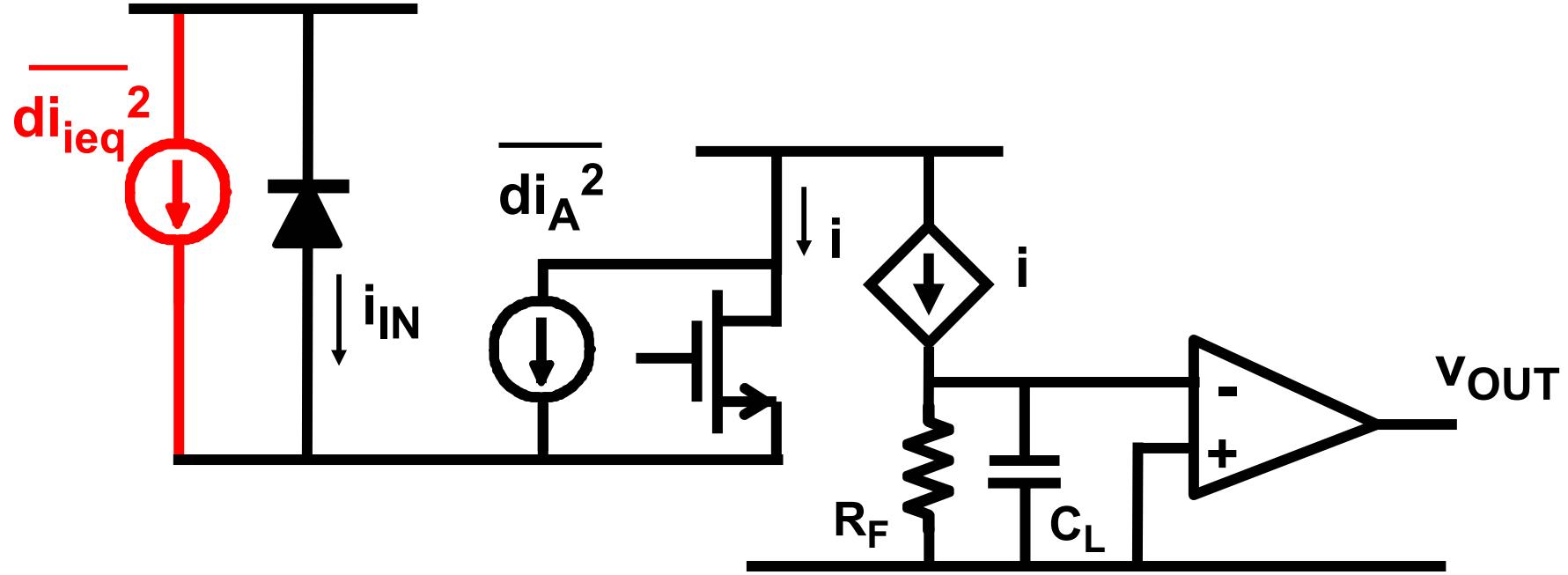
Noise sources of detector current amplifier



$$\overline{di_D^2} = 2q I_D df$$

$$\overline{di_A^2} = 4kT \frac{2}{3} g_m df$$

Noise density of detector current amplifier



$$\overline{di_{ieq}^2} = \overline{di_D^2} + 4kT \frac{2}{3} g_m df \quad \text{is transistor noise !}$$

Comparison of noise densities

Voltage amp.: $\overline{i_{IN}^2} = \overline{di_R^2} = \frac{4kT}{R_F} df$

Current amp.: $\overline{i_{IN}^2} = \overline{di_A^2} = 4kT \frac{2}{3} g_m df$

 **Voltage amplifier better when $R_F > \frac{3}{2} \frac{1}{g_m}$**

Comparison of integrated noise

Large I_D : $\overline{i_{IN}^2} = \overline{di_D^2} (\text{BW} \frac{\pi}{2})$

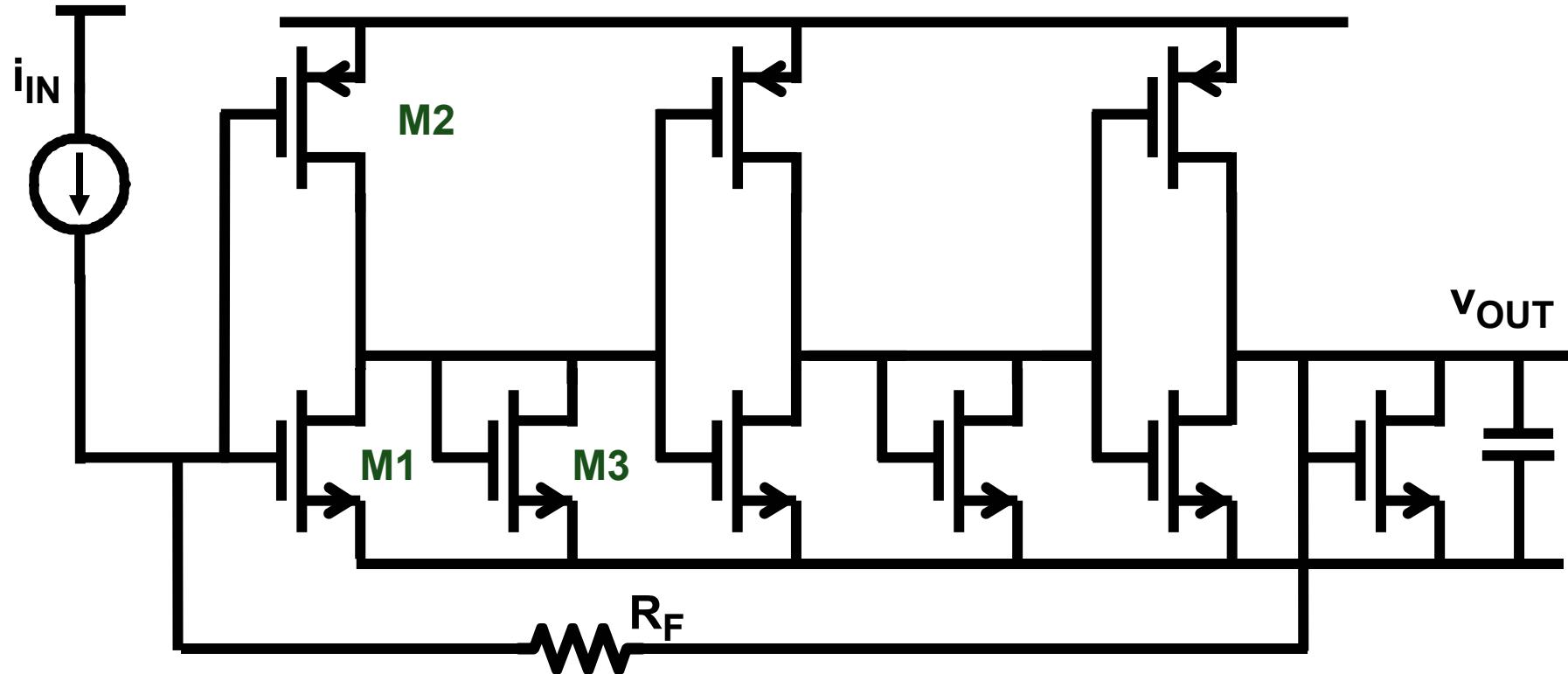
Small I_D :

Voltage amp.: $\overline{i_{IN}^2} = \overline{di_R^2} (\text{BW} \frac{\pi}{2}) = \frac{kT}{R_L} \left(\frac{R_L}{R_F}\right)^2 \frac{g_m}{C_P}$

Current amp.: $\overline{i_{IN}^2} = \overline{di_A^2} (\text{BW} \frac{\pi}{2}) = \frac{2}{3} \frac{kT}{R_F} \frac{g_m}{C_L}$

 **Voltage amplifier better when $R_F > \frac{3}{4} R_L$**

CMOS photodiode amplifier



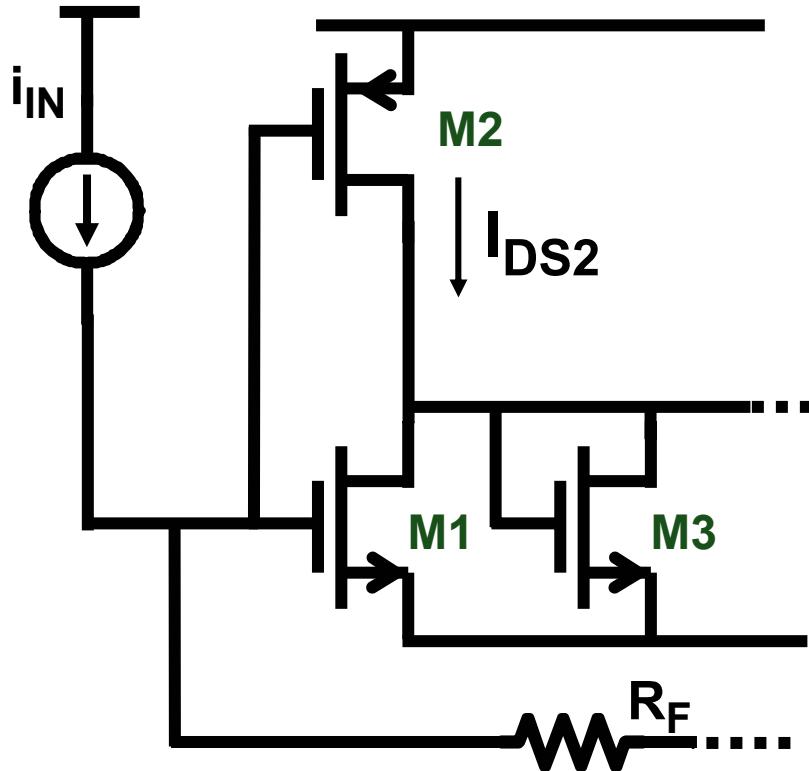
$$150 \text{ k}\Omega \times 120 \text{ MHz} = 18 \text{ THz}\Omega$$

450 MHz per cell

$$0.5 \text{ pA}/\sqrt{\text{Hz}}$$

Ref. Ingels, JSSC Dec 1994, 1552-1559

CMOS wideband amplifier cell



M_1 & M_3 : same V_{GS} & V_{DS}

$K'_n \approx 2K'p$

All L are L_{min}

$$A_v = \frac{g_{m1} + g_{m2}}{g_{m3}}$$

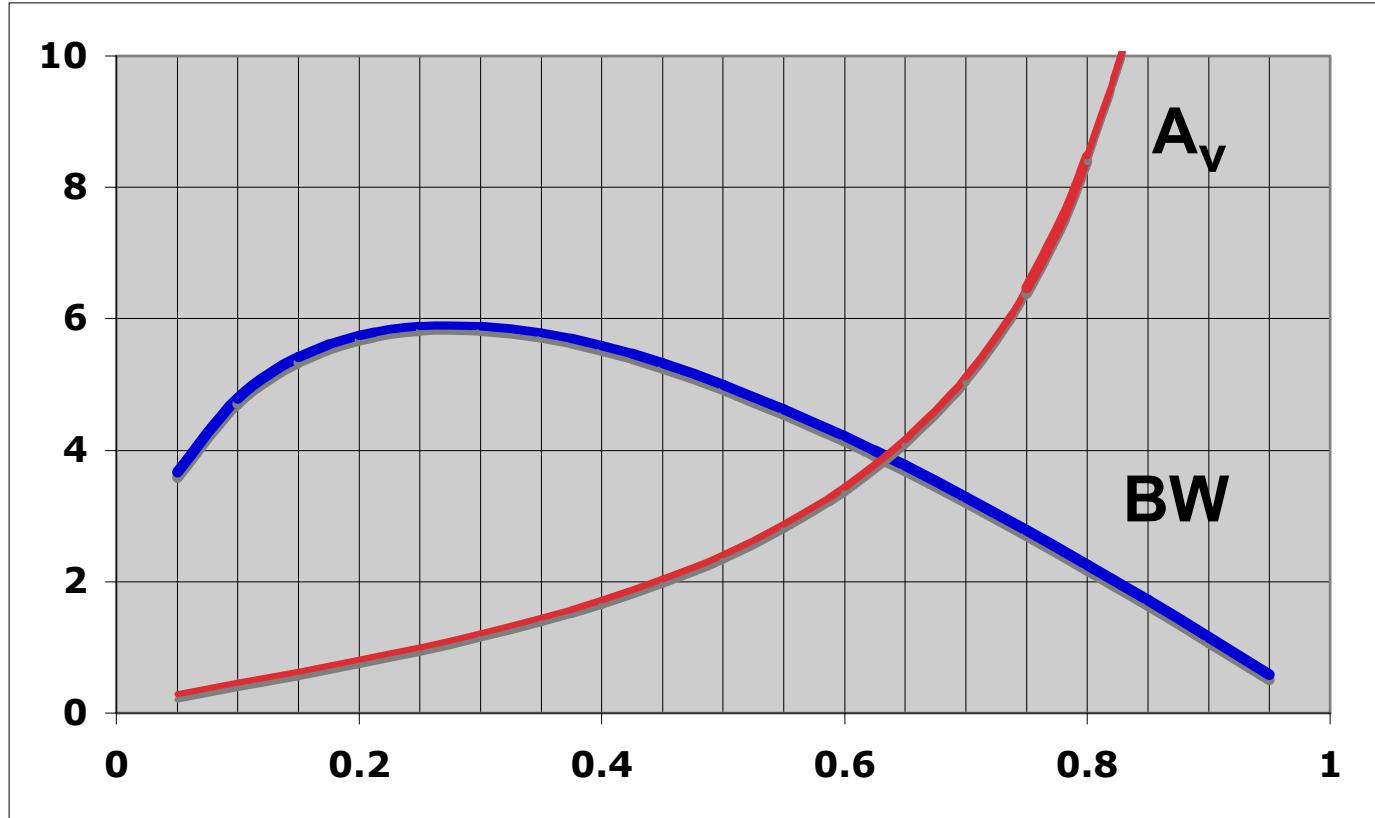
$$g_m = 2 \sqrt{K' n I_{DS} W/L}$$

$$I_{DS1} = \lambda I_{DS2}$$

$$I_{DS3} = (1 - \lambda) I_{DS2}$$

$$V_{GS1} = V_{GS3} : W_3 = W_1 \frac{1 - \lambda}{\lambda}$$

CMOS wideband amplifier : gain and bandwidth



$$\frac{\lambda}{1 - \lambda} \left(1 + \sqrt{\frac{W_2}{2\lambda W_1}} \right)$$

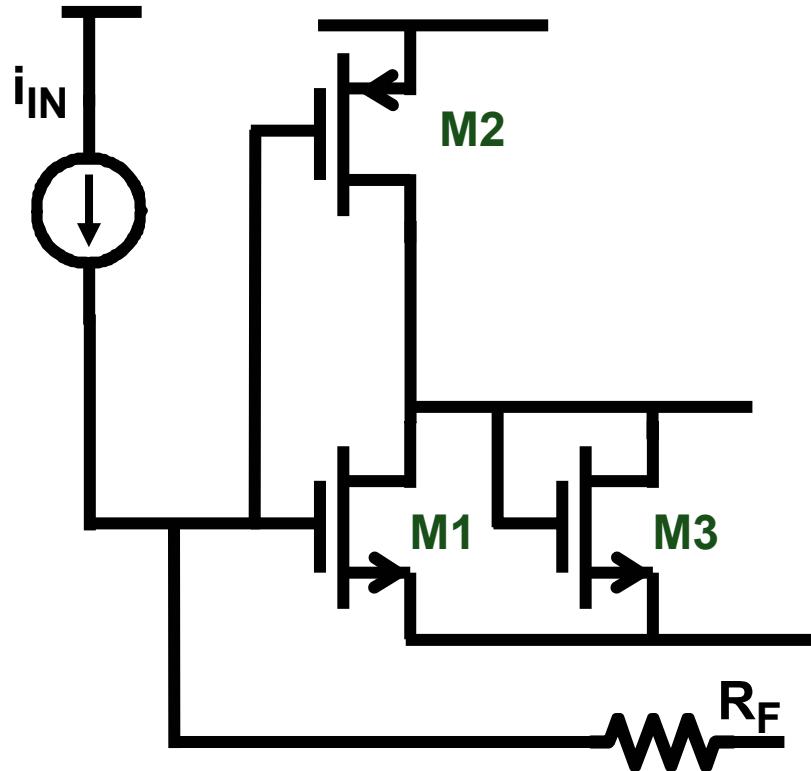
$$BW = \frac{g_{m3}}{2\pi C_n}$$
$$\sim \frac{(1 - \lambda) \sqrt{\lambda W_1}}{W_1(2 - \lambda) + \lambda W_2}$$

λ

$$W_1 = 2$$
$$W_2 = 4$$

$$C_n = C_{DB1} + C_{GS3} + C_{DB3} + C_{DB2}$$
$$C_{DB} \approx C_{GS} \approx kW \quad k \approx 2 \text{ fF}/\mu\text{m}$$

Integrated resistor



R_F ? Poly R : large size : large L
distributed C :
 45° phase shift at 100 MHz

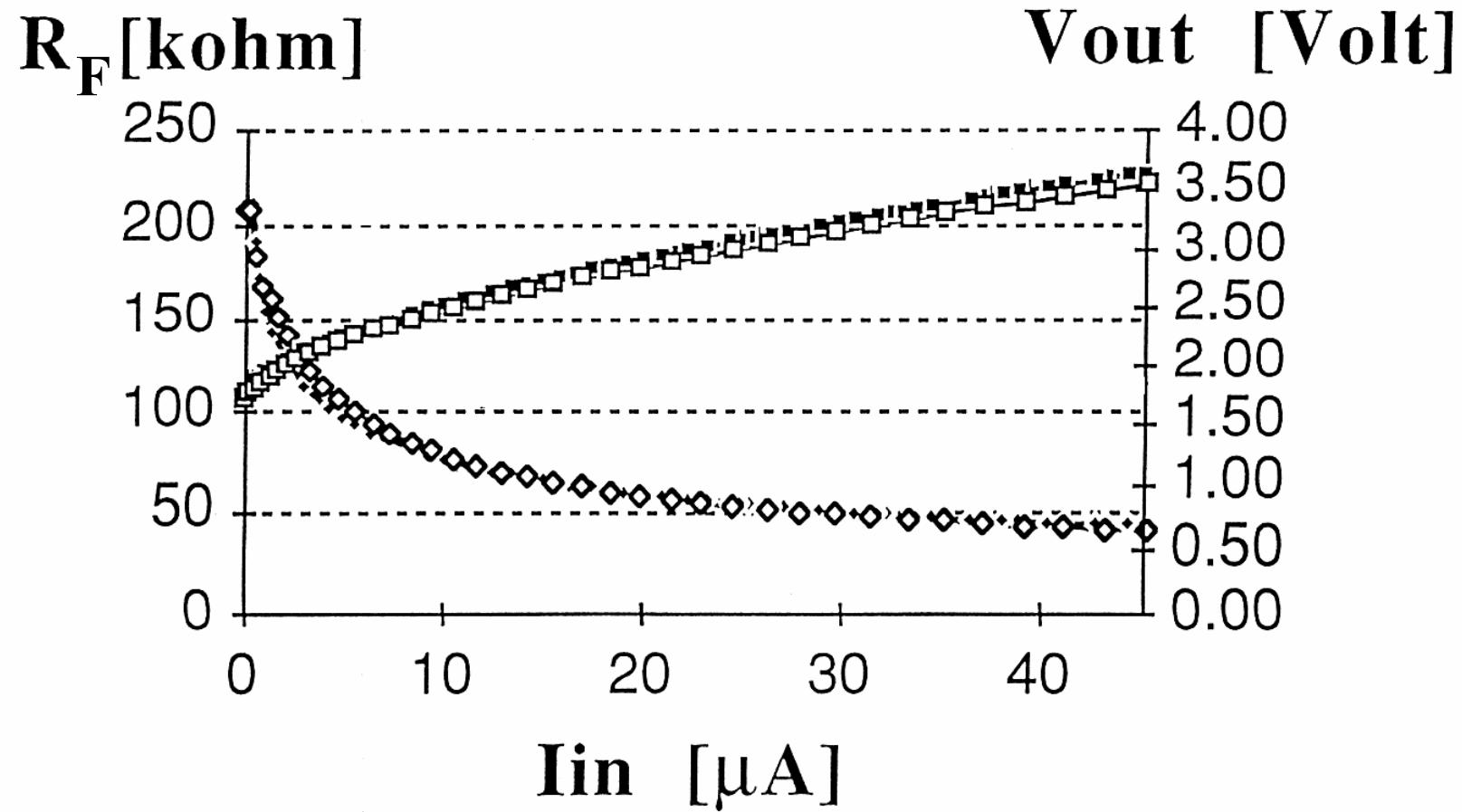
$$f_{-3\text{dB}} = \frac{1}{2\pi} \frac{2.43}{R_s C_0 L^2}$$

R_s = sheet res. (Ω / \square)
 C_0 = unit cap. (F/cm^2)

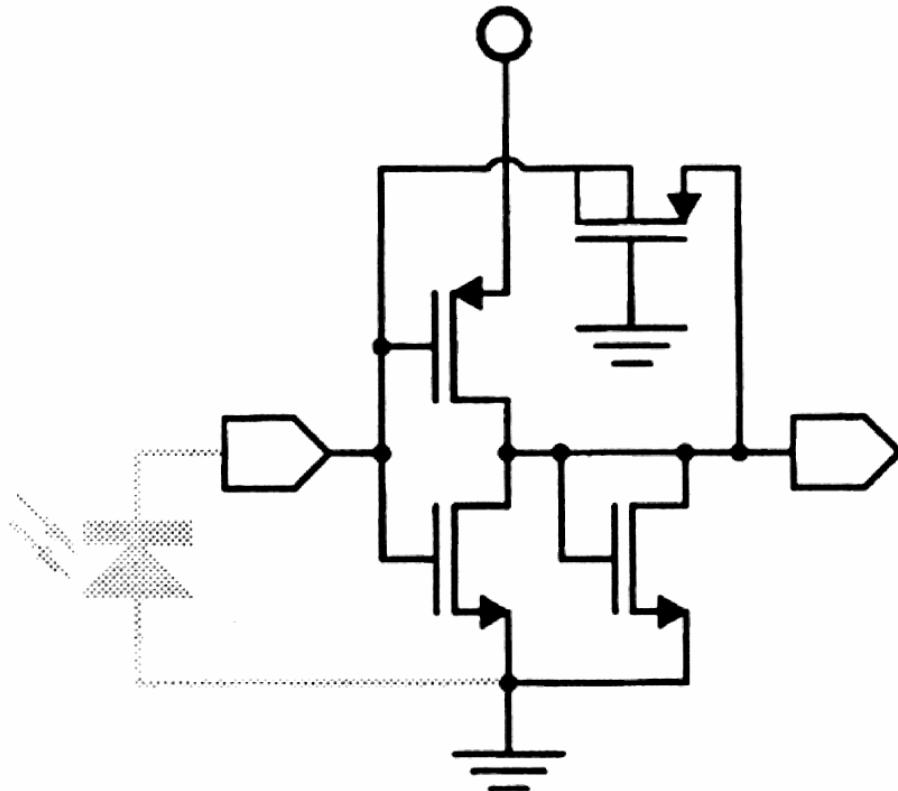
MOST : $W = 1.3 \mu\text{m}$ & $L = 1 \mu\text{m}$
allows dynamic compression

Glaser; IC Engineering
Add.Wesley, p.132

Gain compression



1 Gb/s 1 kΩ transimpedance stage



pMost vs nMOST :

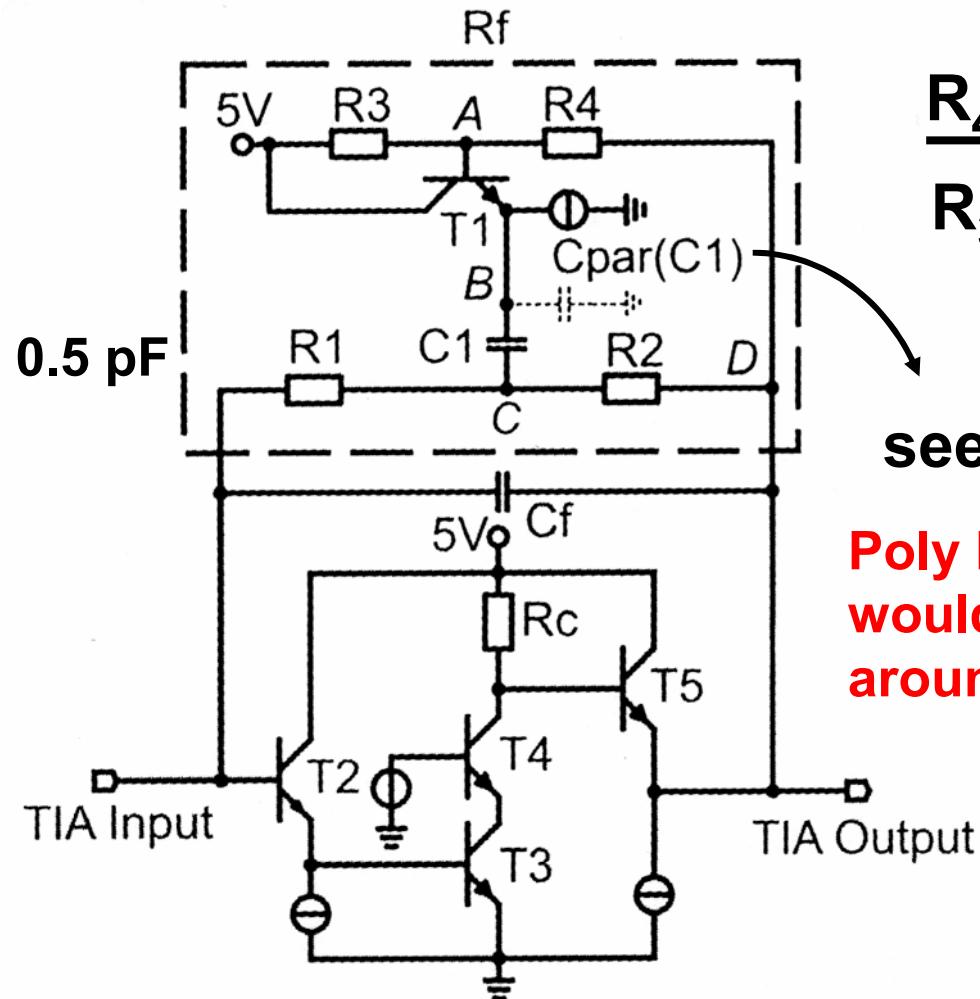
nMOST R increases for
larger diode currents !
pMOST gives compression !

$C_d = 0.8 \text{ pF} \approx C_{GS}$
Capacitive noise matching !

BW = 500 MHz
5 mA (5V)
0.7 μm CMOS

Ref. Ingels, JSSC July 1999, 971-977

High-frequency Resistance RF



$$\frac{R_4}{R_3} = \frac{R_2}{R_1} = 2$$

sees $1/g_m 1$

Poly $R_F = 200 \text{ k}\Omega$
would cut off
around 67 MHz !

$$R_1 + R_2 = 200 \text{ k}\Omega$$

$$R_3 + R_4 = 4 \text{ k}\Omega$$

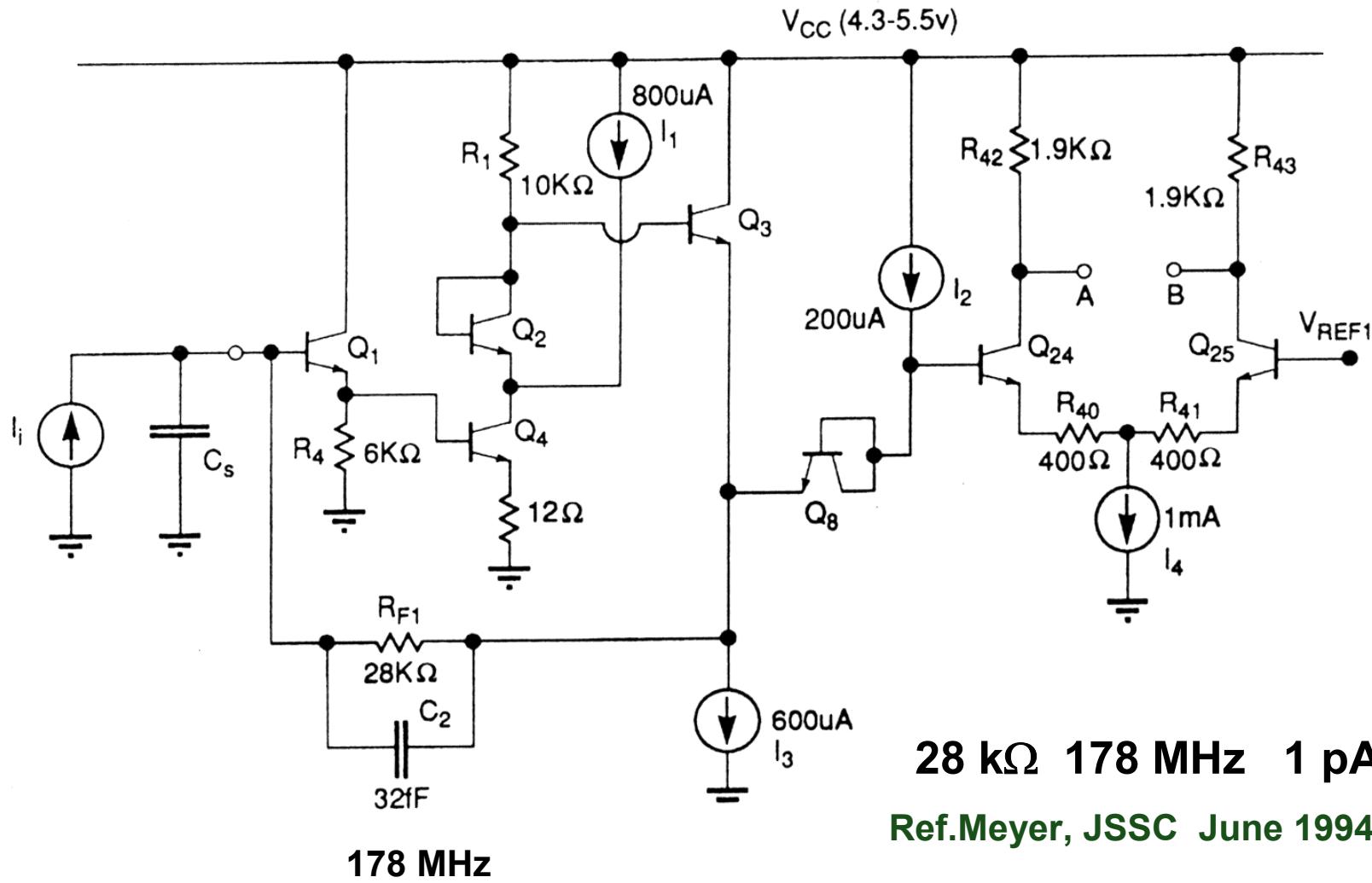
$$C_d = 0.1 \text{ pF}$$

$$180 \text{ k}\Omega \quad 380 \text{ MHz} \\ 68 \text{ THz}\Omega$$

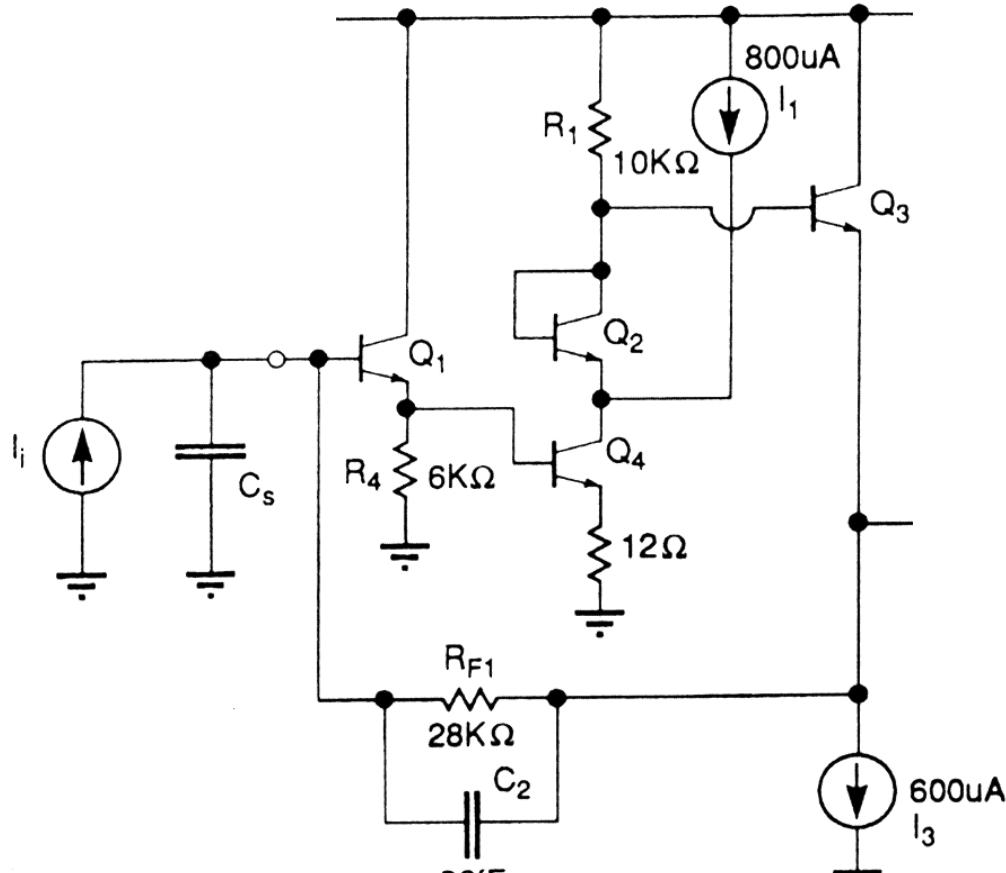
14 mA (5 V)
0.6 μm BiCMOS

Seidl, ISSCC 04, 470-471

BICMOS transimpedance amplifier



BICMOS transimpedance amplifier



178 MHz

$$A_v = \frac{R_1 // ..}{12 + 1/g_{m4}} = \frac{5 \text{ k}\Omega}{12 + 28} = 125$$

$$R_i = \frac{R_{F1}}{1 + A_v} = 240 \Omega$$

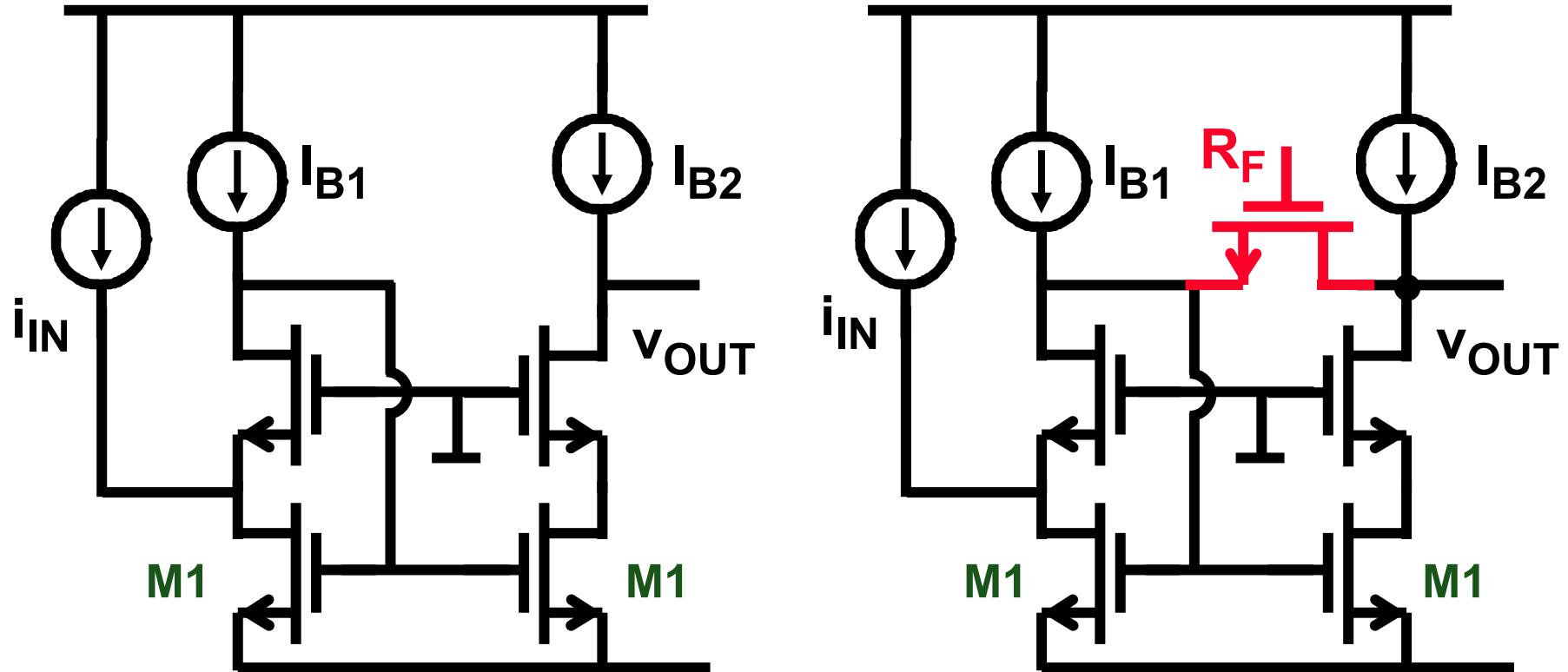
$$C_i = (1 + A_v) C_2 = 4 \text{ pF}$$

$$\overline{di^2} = 2qI_B df + \frac{4kT}{R_{F1}} df \\ = (0.4 + 0.6)10^{-24} \approx 10^{-24} \text{ A}^2/\text{Hz}$$

$$28 \text{ k}\Omega \quad 178 \text{ MHz} \quad 1 \text{ pA}_{\text{RMS}}/\sqrt{\text{Hz}}$$

Ref.Meyer, JSSC June 1994, 701-706

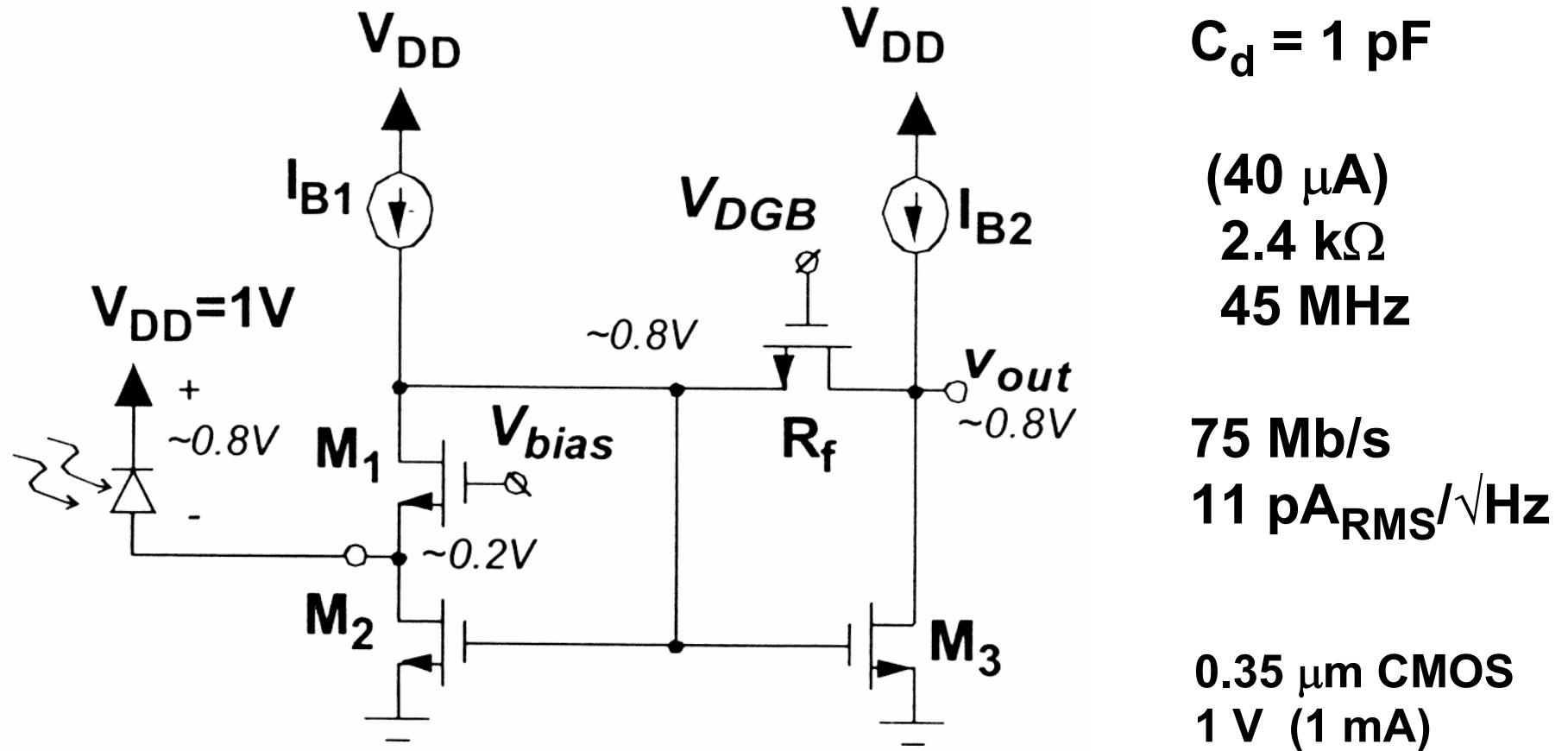
Low-voltage transimpedance amplifier



$$\text{If } R_F > 1/g_m : v_{OUT} = -R_F i_{IN}$$

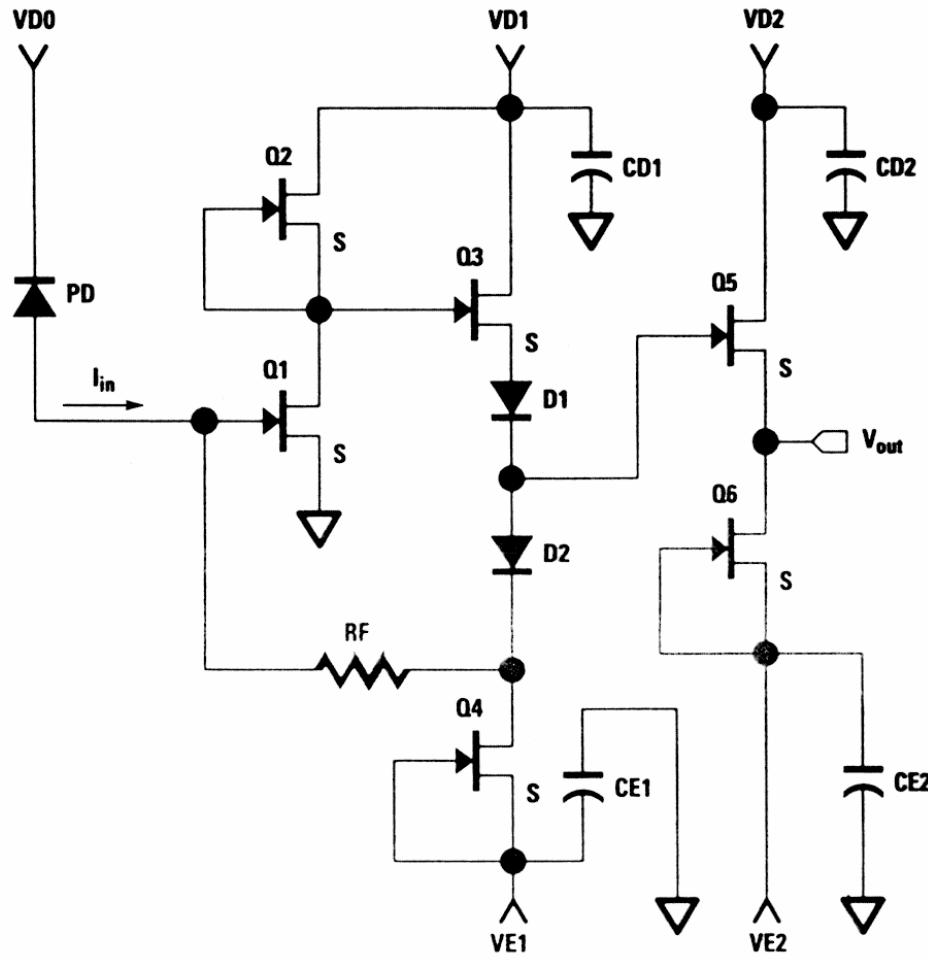
Ref.Phang, Johns, ISSCC 2001, 218-219

75 Mb/s optical receiver in CMOS



Ref. Phang, ISSCC 2001 218-219

GaAs 10 Gb/s receiver



HP - GaAs MODIC :
depletion nMOS'T's

560 V/W

flip-chip PD :
-3 dB at 7.2 GHz
10 pA/ $\sqrt{\text{Hz}}$

wire bond :
-3 dB at 4.2 GHz
20 pA/ $\sqrt{\text{Hz}}$

Table of contents

- **Introduction**
- **Shunt-shunt FB for Transimpedance amps.**
- **Shunt-series FB for Current amplifiers**
- **Transimpedance amplifiers for
low noise and high frequencies**